

# Evidence for spin-fluctuation-mediated superconductivity in $n$ -doped cuprates

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EMFL User Meeting  
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# Acknowledgements



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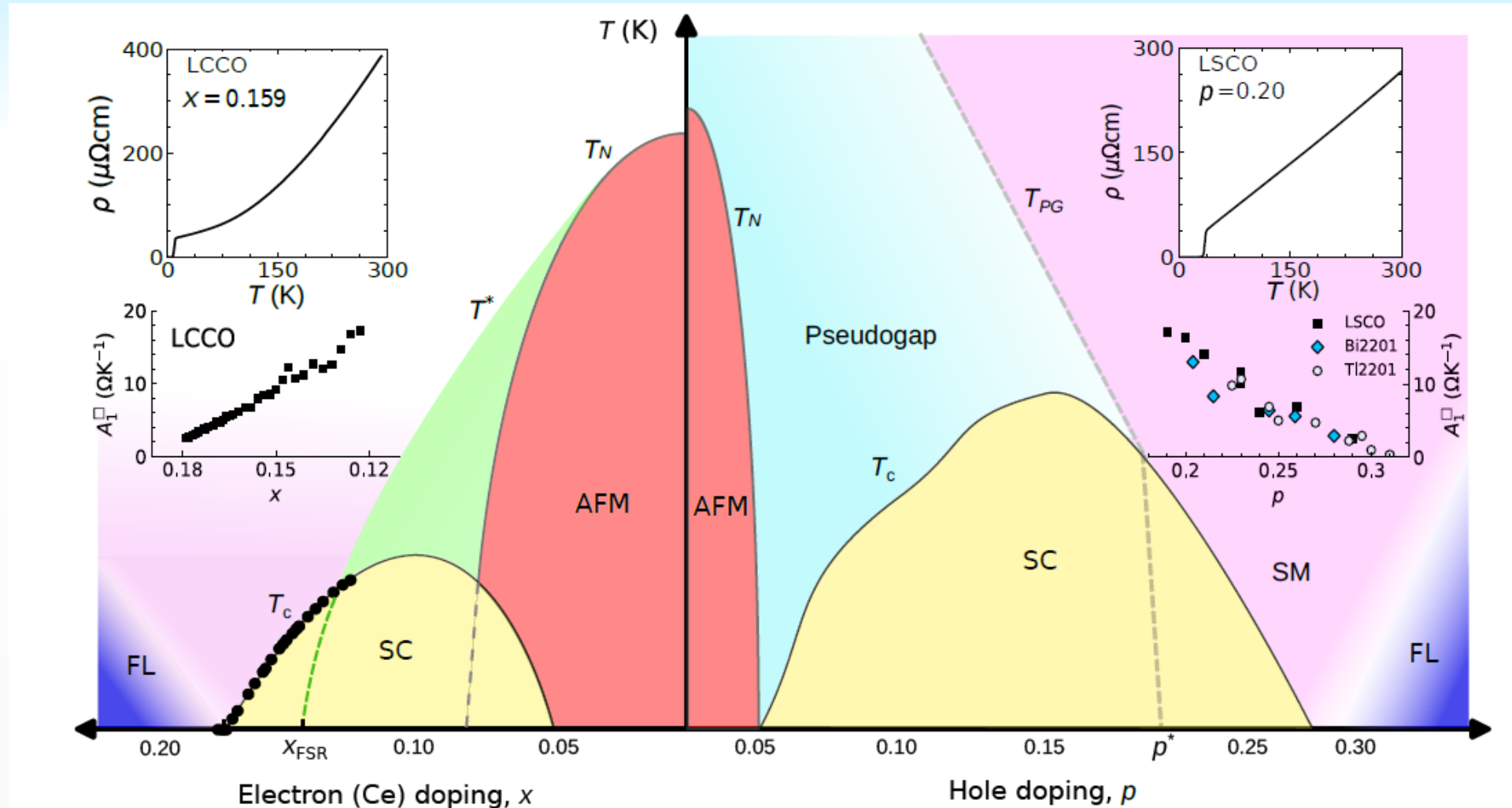


Nigel Hussey

Alessandro Cuoghi



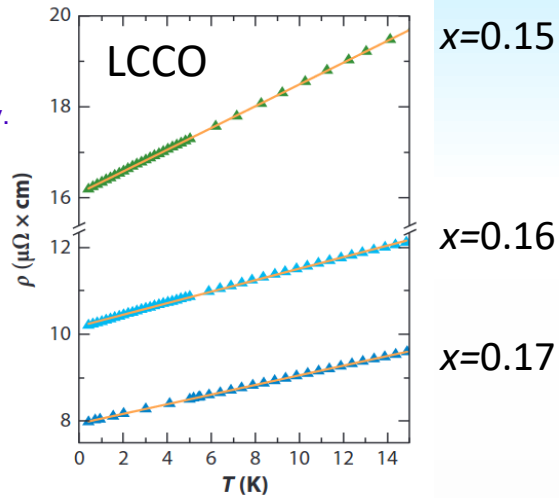
# Phase diagram



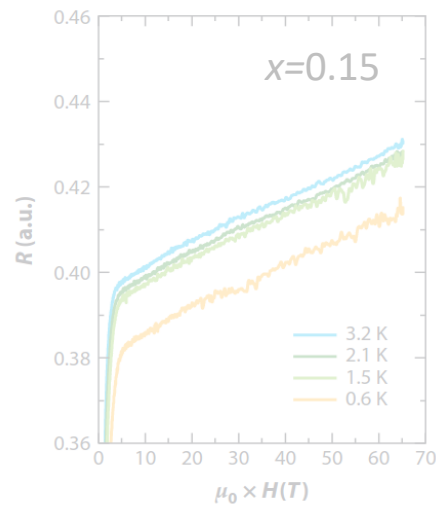
# Similarities...

T. Sarkar *et al.*, *Sci. Adv.* **5**:eaav675 (2019)

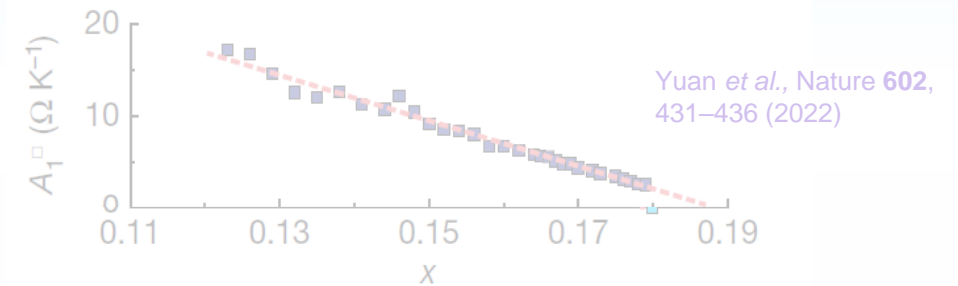
*T*-linear resistivity



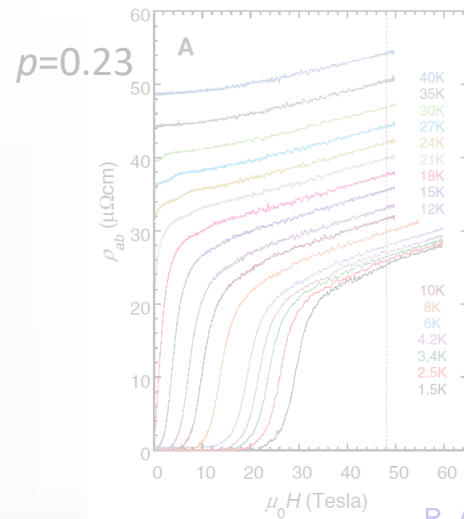
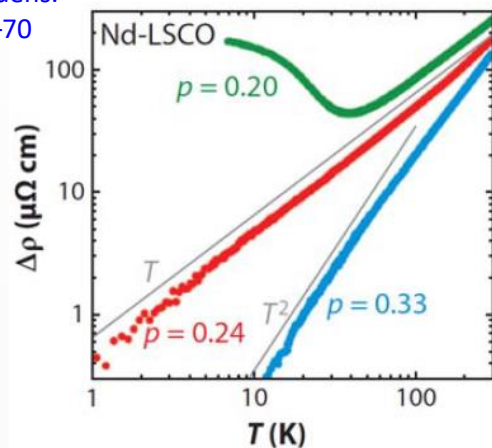
*H*-linear magnetoresistance



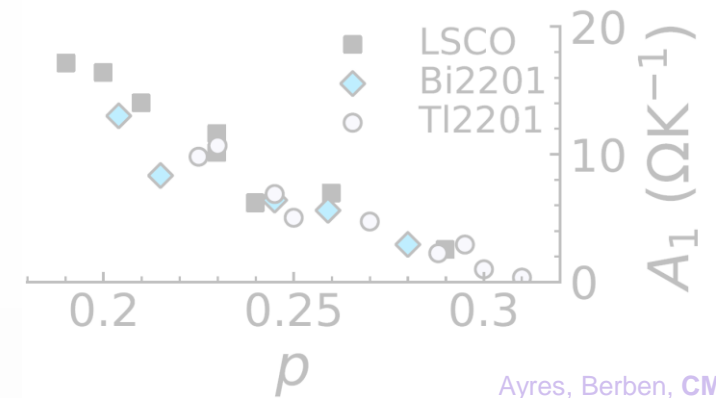
Scaling of *T*-linear resistivity and  $T_c$



Taillefer, *Annu. Rev. Condens. Matter Phys.* 2010. 1:51–70



R. A. Cooper *et al.*, *Science* **323**, 603–607 (2009)

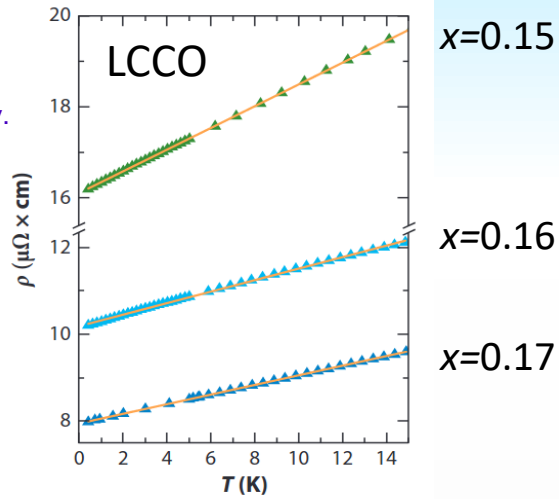


Ayres, Berben, *CMD*, *et al.*, arXiv:2203.04867

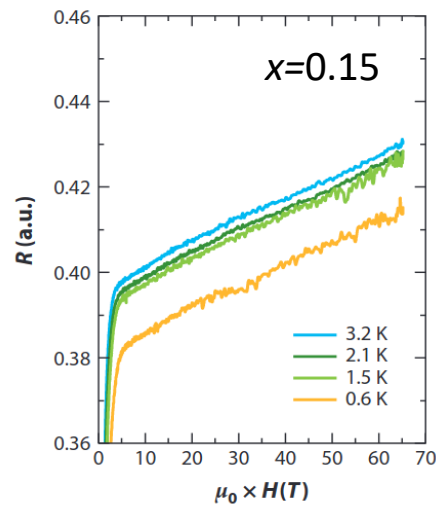
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T. Sarkar *et al.*, *Sci. Adv.* **5**:eaav675 (2019)

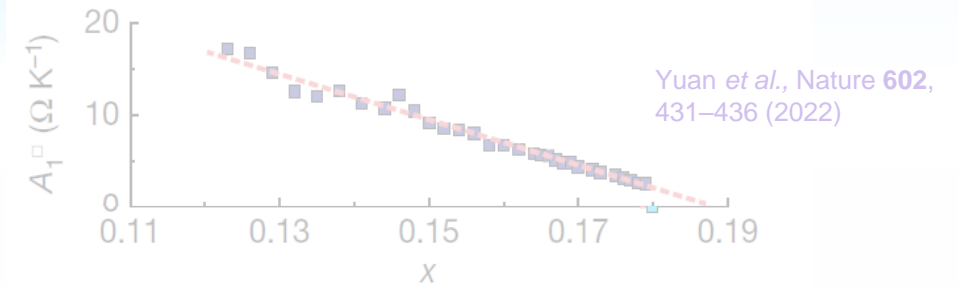
*T*-linear resistivity



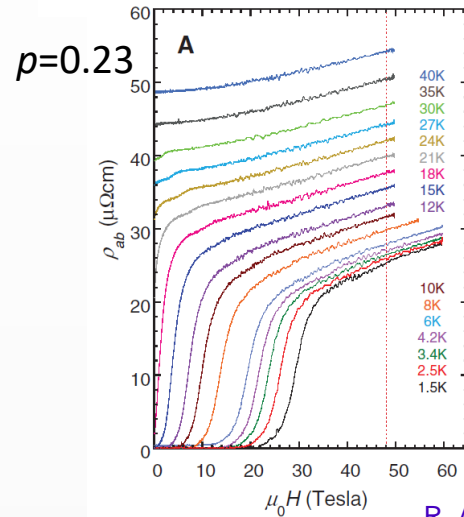
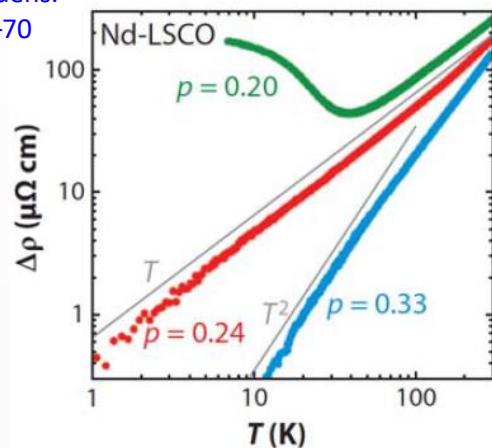
*H*-linear magnetoresistance



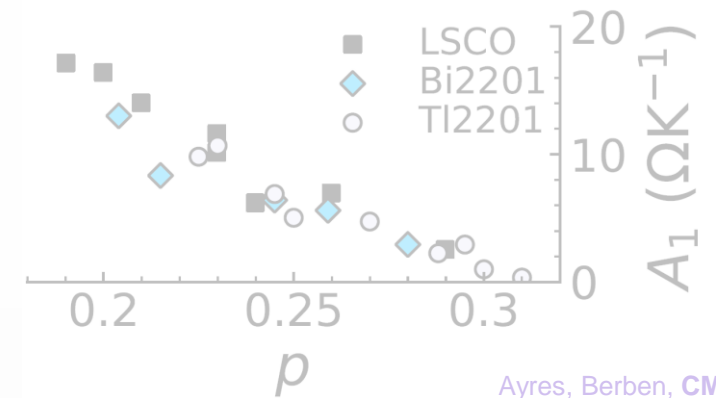
Scaling of *T*-linear resistivity and  $T_c$



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R. A. Cooper *et al.*, *Science* **323**, 603-607 (2009)

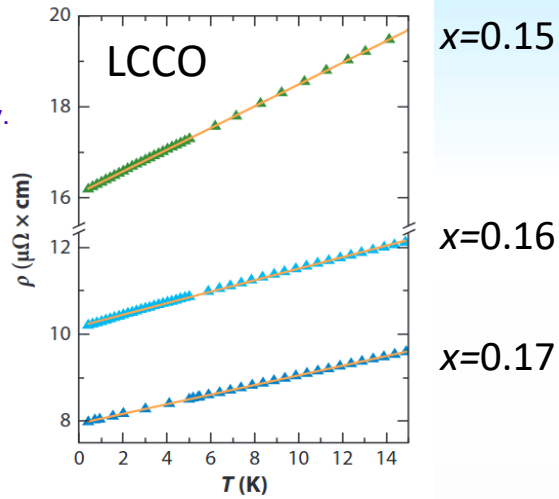


Ayres, Berben, **CMD**, *et al.*, arXiv:2203.04867

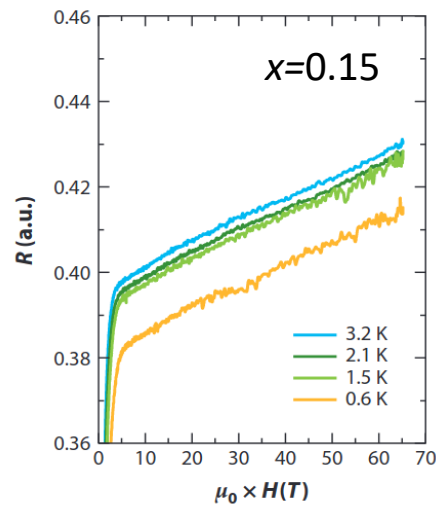
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T. Sarkar *et al.*, *Sci. Adv.* **5**:eaav675 (2019)

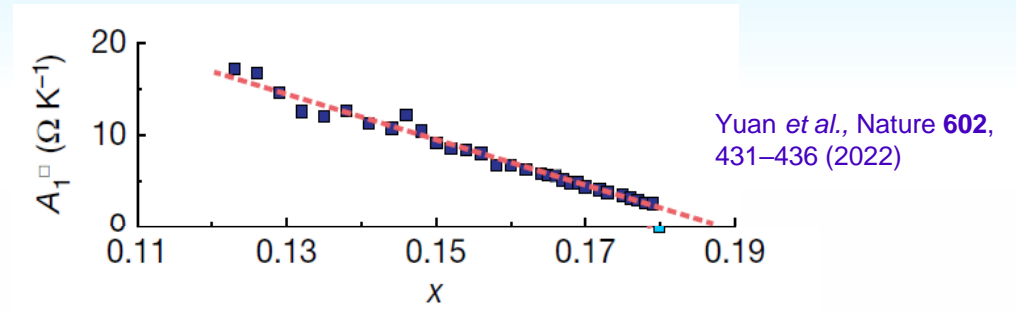
*T*-linear resistivity



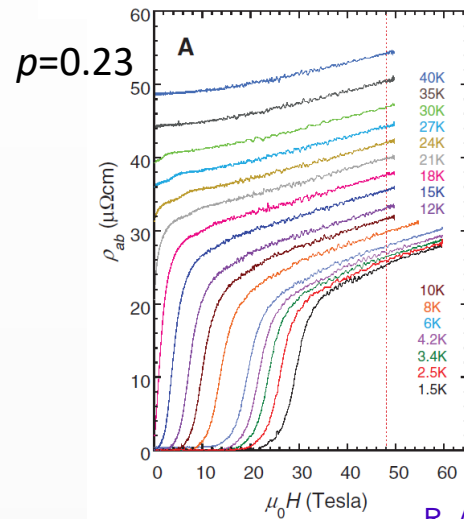
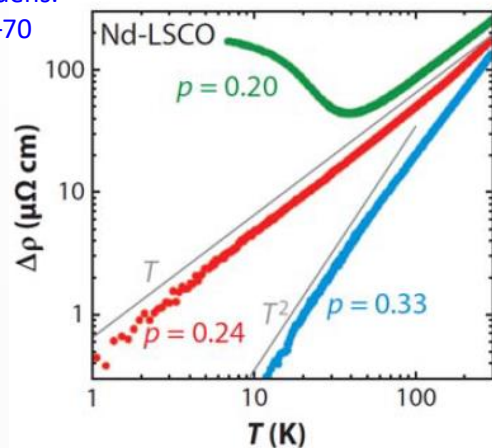
*H*-linear magnetoresistance



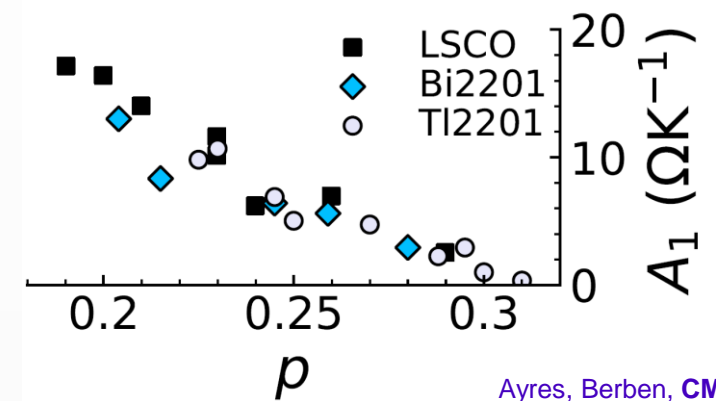
Scaling of *T*-linear resistivity and  $T_c$



Taillefer, *Annu. Rev. Condens. Matter Phys.* 2010. 1:51–70



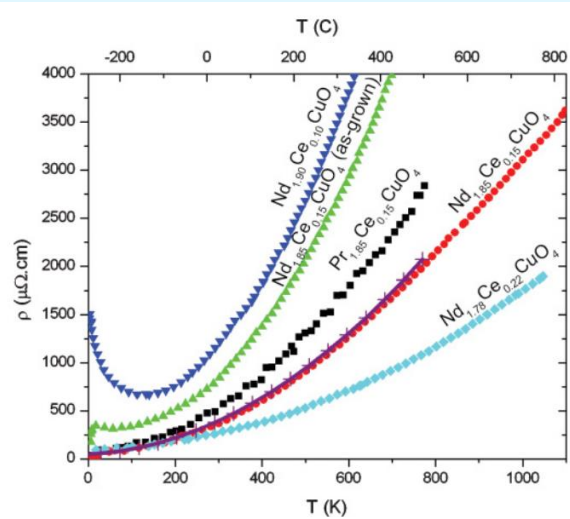
R. A. Cooper *et al.*, *Science* **323**, 603-607 (2009)



Ayres, Berben, **CMD**, *et al.*, arXiv:2203.04867

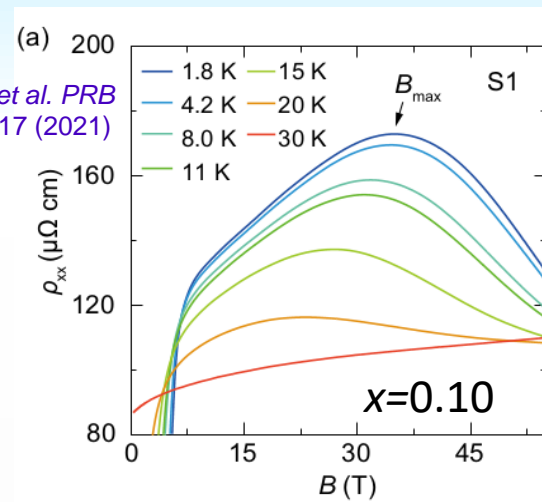
# ...and differences

Quadratic resistivity at high- $T$ .



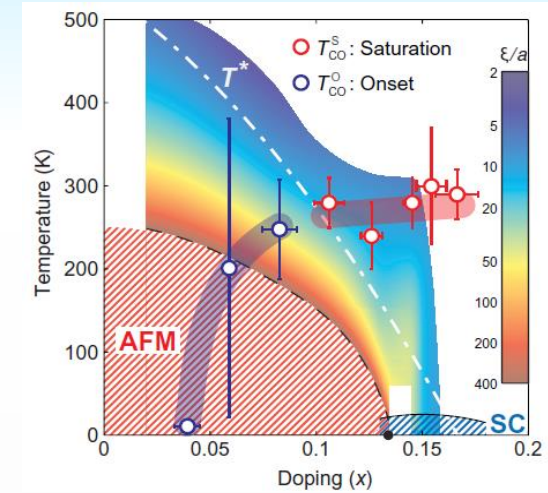
P.L. Bach *et al.*, PRB **83**, 212506 (2011)

Non-trivial MR in the AFM phase.

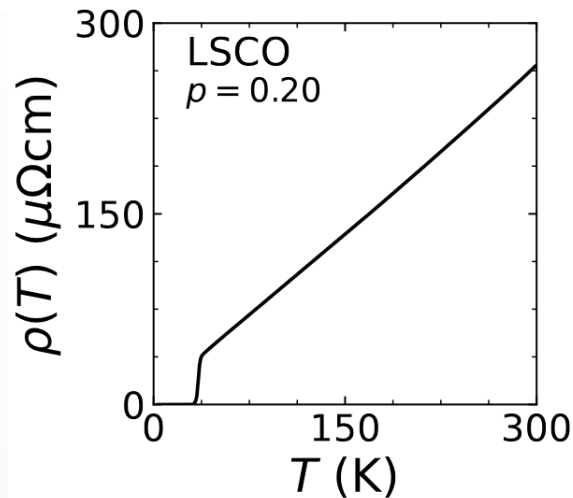


X. Zhang *et al.* PRB **103**, 014517 (2021)

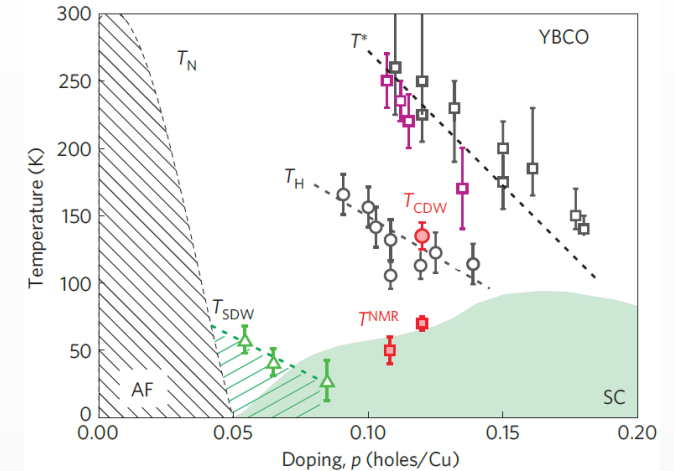
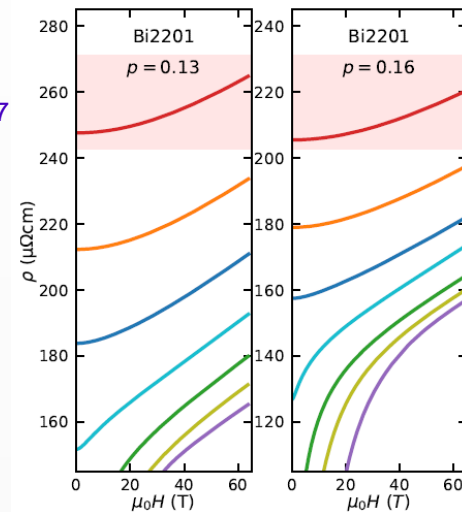
Minimal influence from CO.



da Silva Neto *et al.*, Sci. Adv. 2016; 2 : e1600782



Ayres, Berben, CMD, *et al.*, arXiv:2203.04867



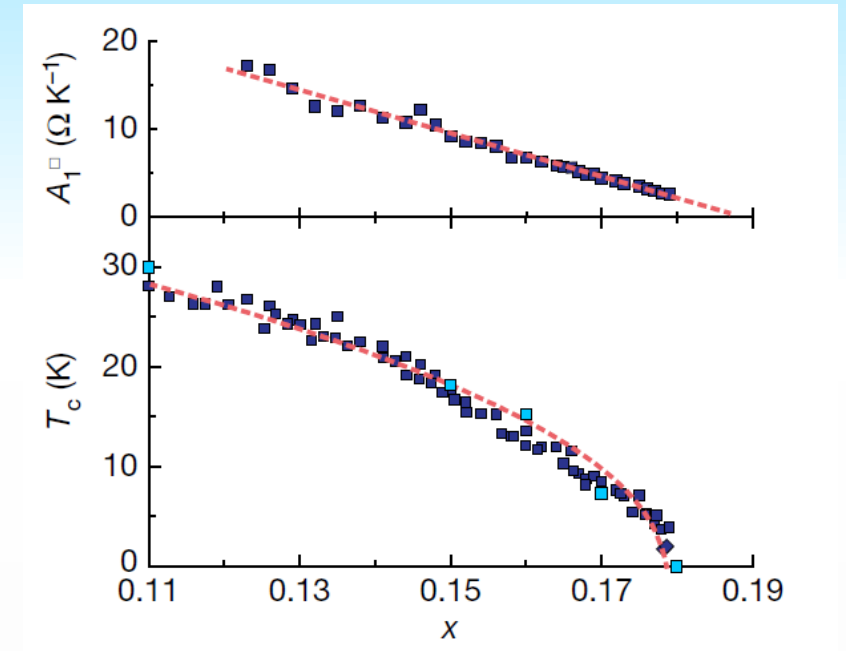
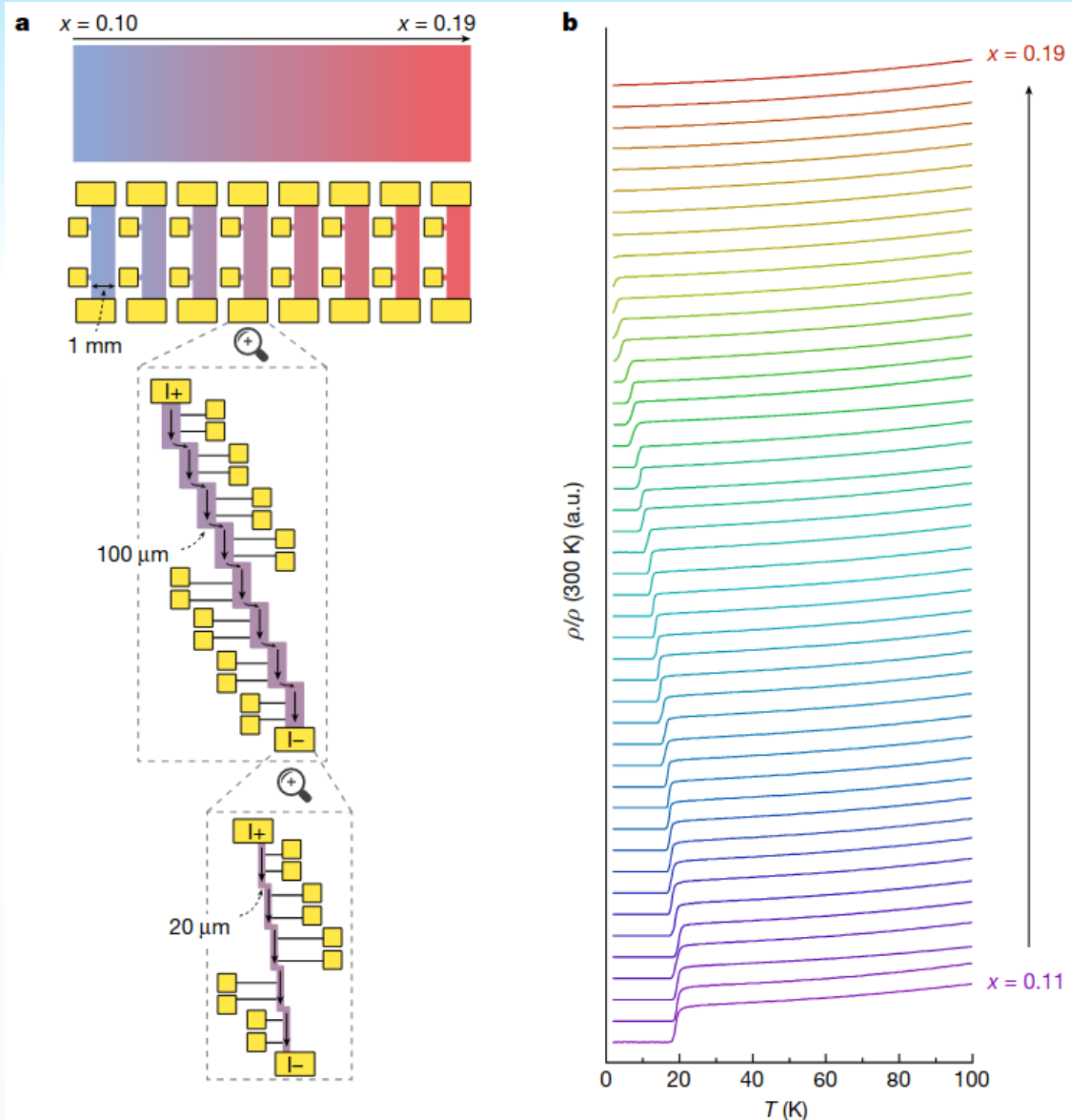
Chang *et al.*, Nat. Phys. **8**, 871-876 (2012)

How can we understand these differences  
between the electron- and hole-doped cuprates?

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# Combinatorial films

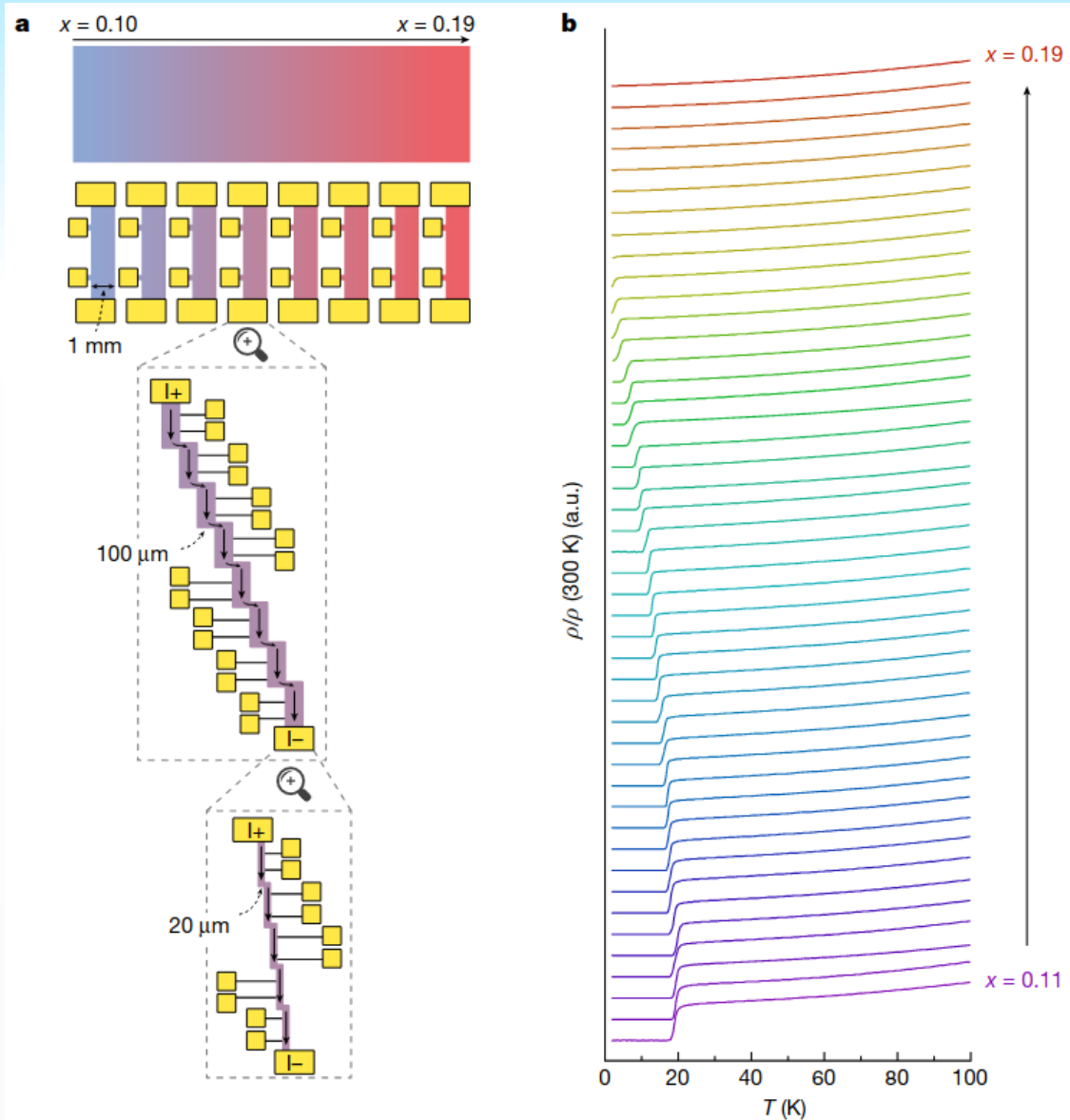


Combi thin films:

- Many doping levels across a single film
- Facilitates very systematic studies

Yuan *et al.*, *Nature*  
602, 431–436 (2022)

# Combinatorial films

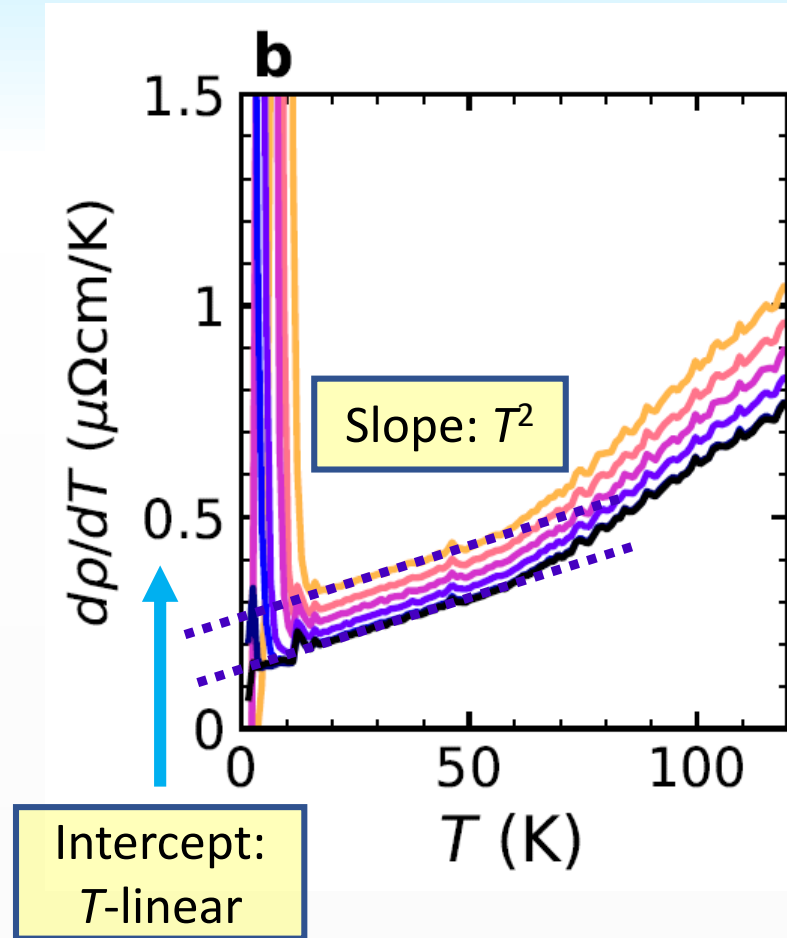
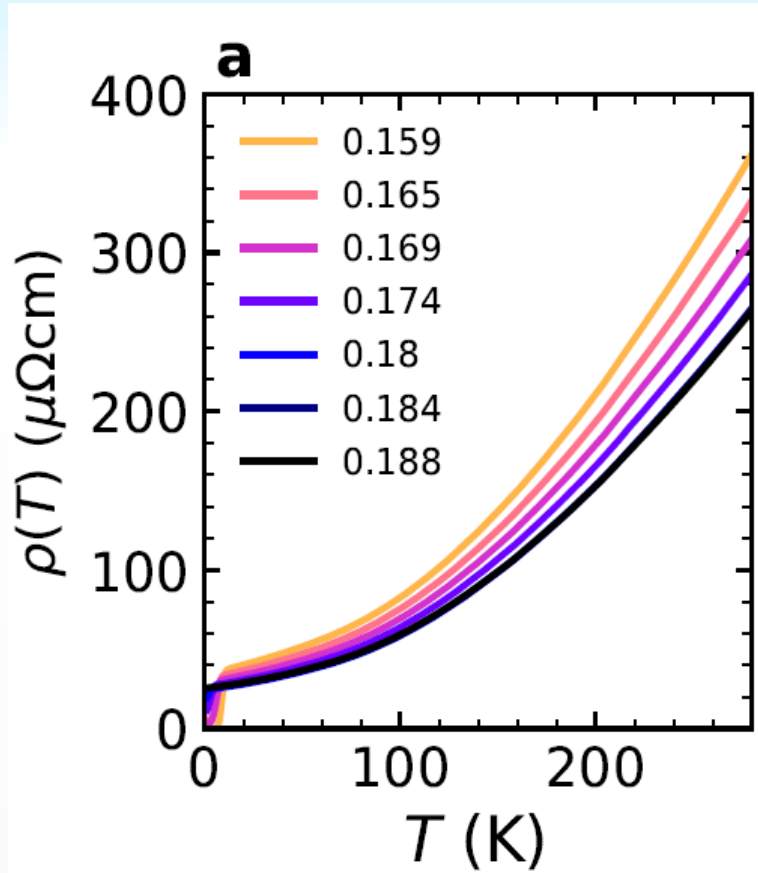


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Yuan *et al.*, *Nature*  
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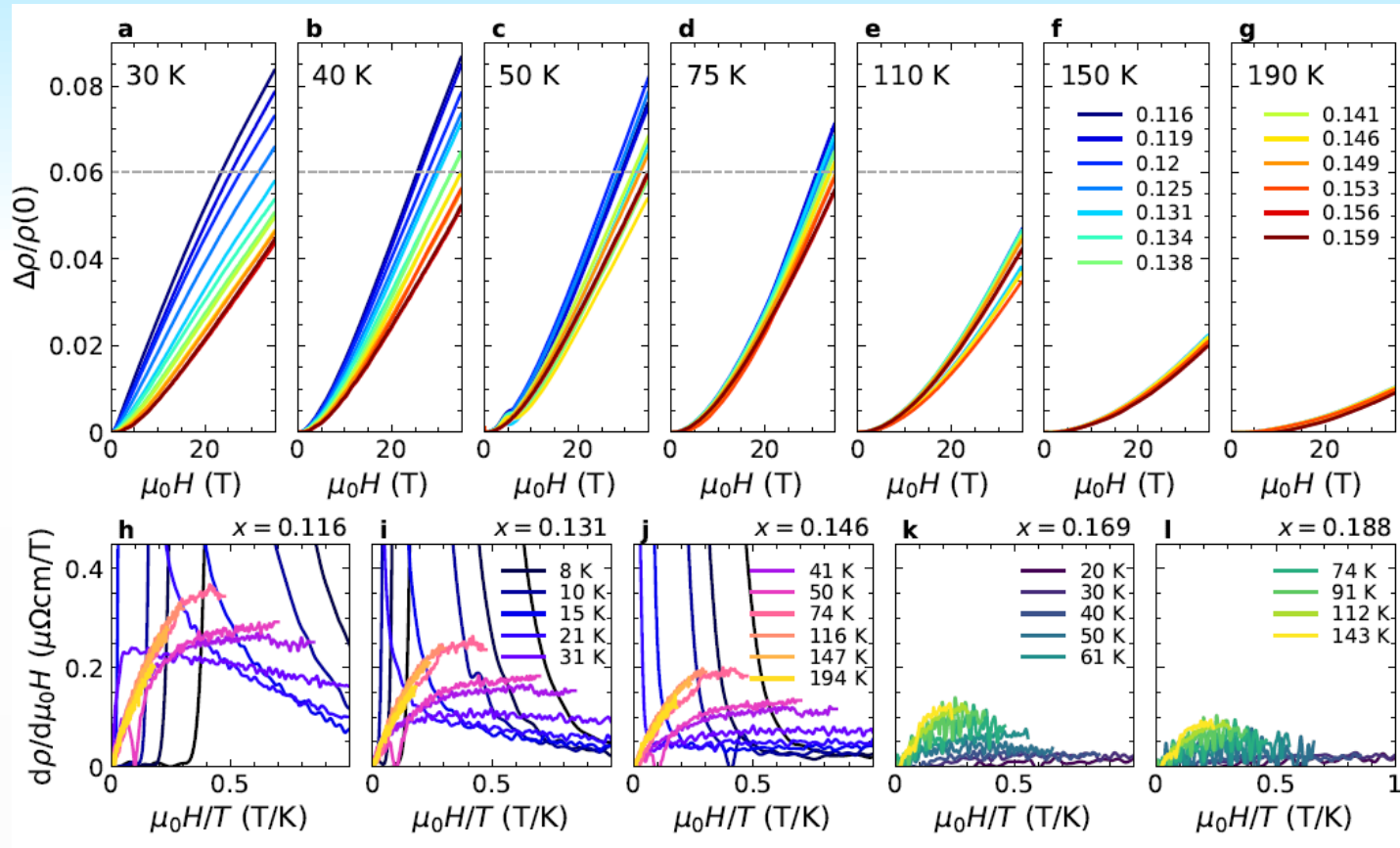
# Zero-field



Intercept ( $T$ -linear component) is  **$x$ -dependent**

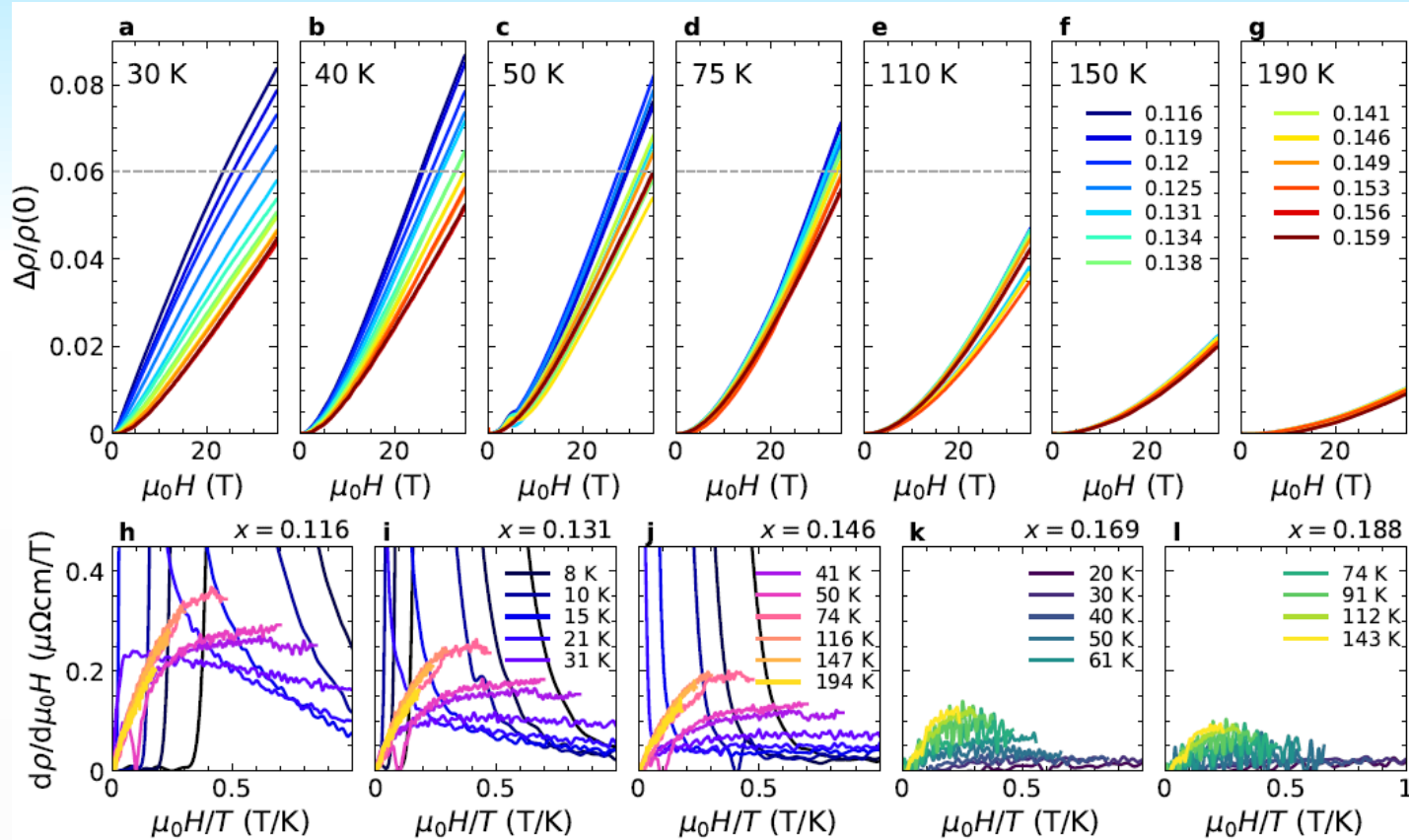
Slope ( $T^2$  component) is  **$x$ -independent**

# Magnetoresistance

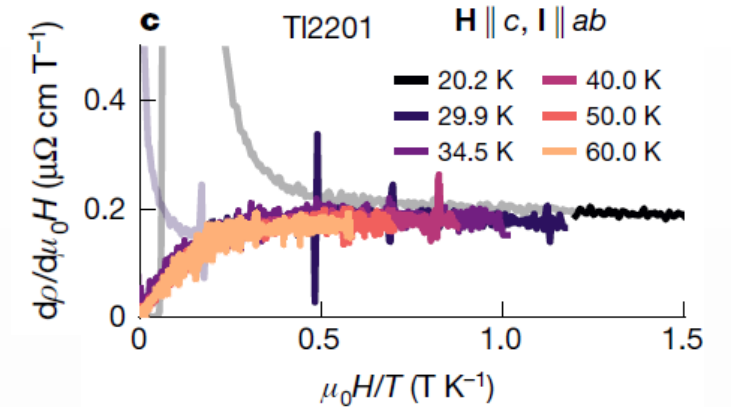


- $H$ -linear MR at high fields for  $x > x_{\text{AFM}}$ .
- The decrease in MR as  $T$  decreases implies that the anisotropy of  $\ell$  decreases faster than  $\ell$  itself.

# Magnetoresistance



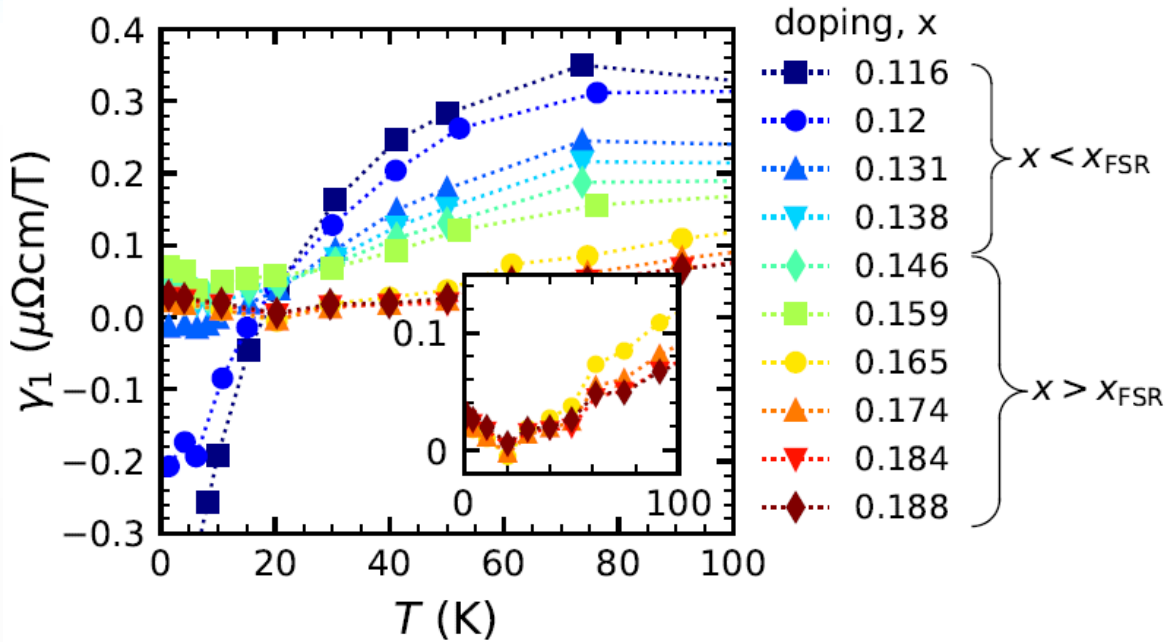
Ayres, Berben, et al.,  
Nature **595**, 661-666 (2021)



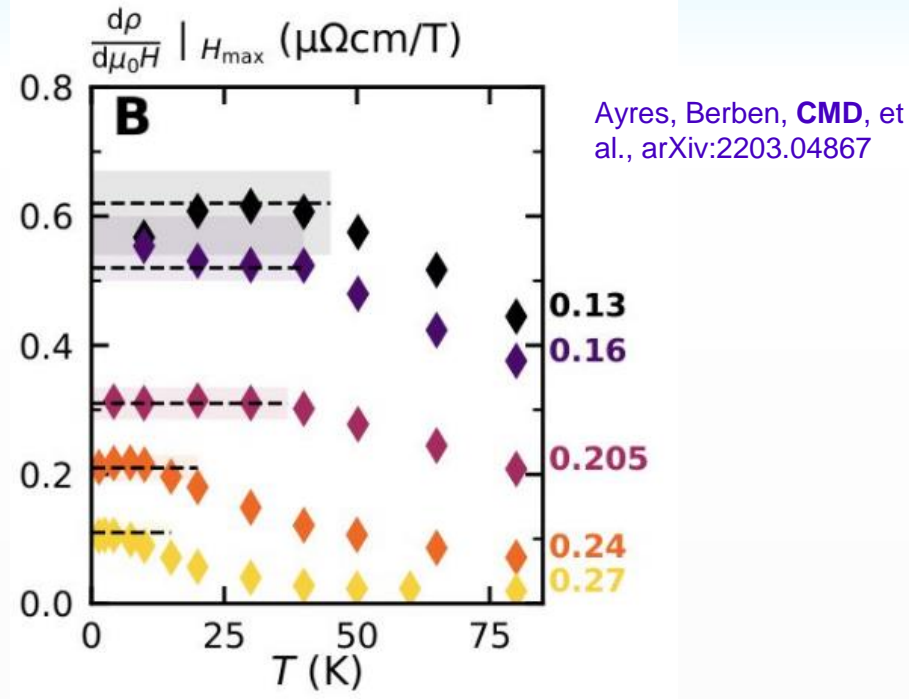
Stark contrast to  $H/T$  scaling seen  
in the  $p$ -doped cuprates

- $H$ -linear MR at high fields for  $x > x_{\text{AFM}}$ .
- The decrease in MR as  $T$  is decreases implies that the anisotropy of  $\ell$  decreases faster than  $\ell$  itself.

# Magnetoresistance



High field slope is always  $T$ -dependent.



In  $p$ -doped cuprates, the high-field slope is scale-invariant.

# Magnetoresistance

Using the data, can we extract a scattering rate that can model the data itself?

Can this provide hints to the origin of the unusual transport?

What does this tell us about superconductivity in  $n$ -doped cuprates?

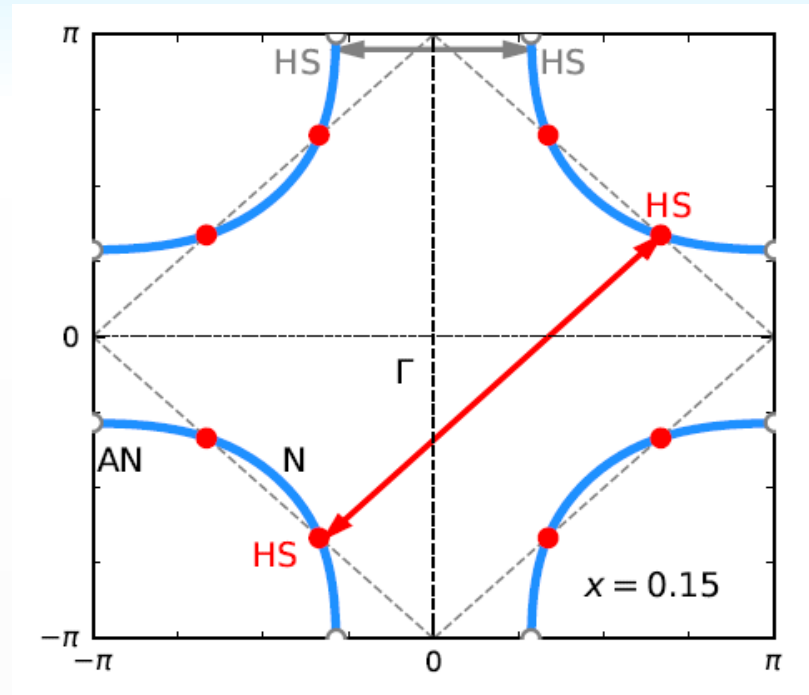
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# Modelling

Solution of Boltzmann Equation for 2D materials:  
Shockley-Chambers Tube Integral Formula

$$\sigma_{ij} = \frac{1}{4\pi^3} \int_{FS} d^2k \frac{1}{\hbar v_F} qv_i \int_0^\infty qv_j(-t) P(t) dt,$$

$$P_\phi(t) := \exp \left[ - \int_0^t \frac{dt'}{\tau(t')} \right]$$



TB params:  
Tang *et al.*, PRB **104**, 155125  
(21)



# Constructing the scattering rate

$$\tau^{-1}(\varphi, T, x) = \tau_{\text{imp}}^{-1} + \tau_{\text{HS}}^{-1}(\varphi) + g(x)\alpha_1 T \sin^2(2\varphi) + \alpha_2 T^2 \sin^2(2\varphi)$$

---

# Constructing the scattering rate

$$\tau^{-1}(\varphi, T, x) = \tau_{\text{imp}}^{-1} + \tau_{\text{HS}}^{-1}(\varphi) + g(x)\alpha_1 T \sin^2(2\varphi) + \alpha_2 T^2 \sin^2(2\varphi)$$

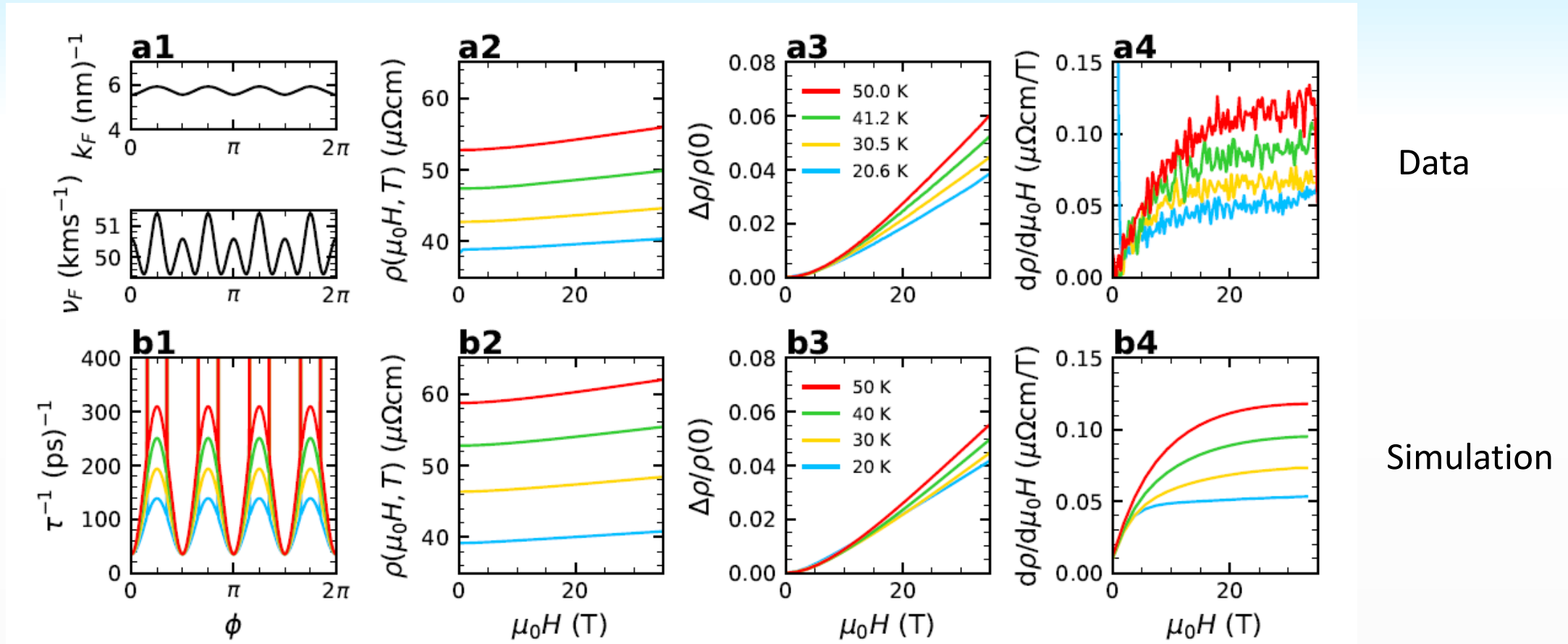
Impurity scattering

Hotspots – required for  $H$ -linear MR

Hinlopen *et al.*, PRR 4, 033195 (2022)

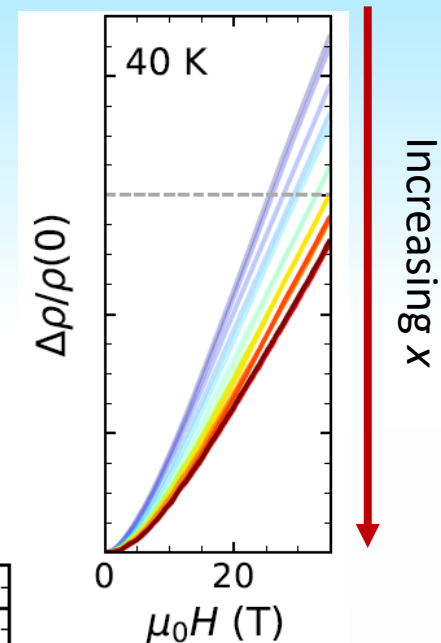
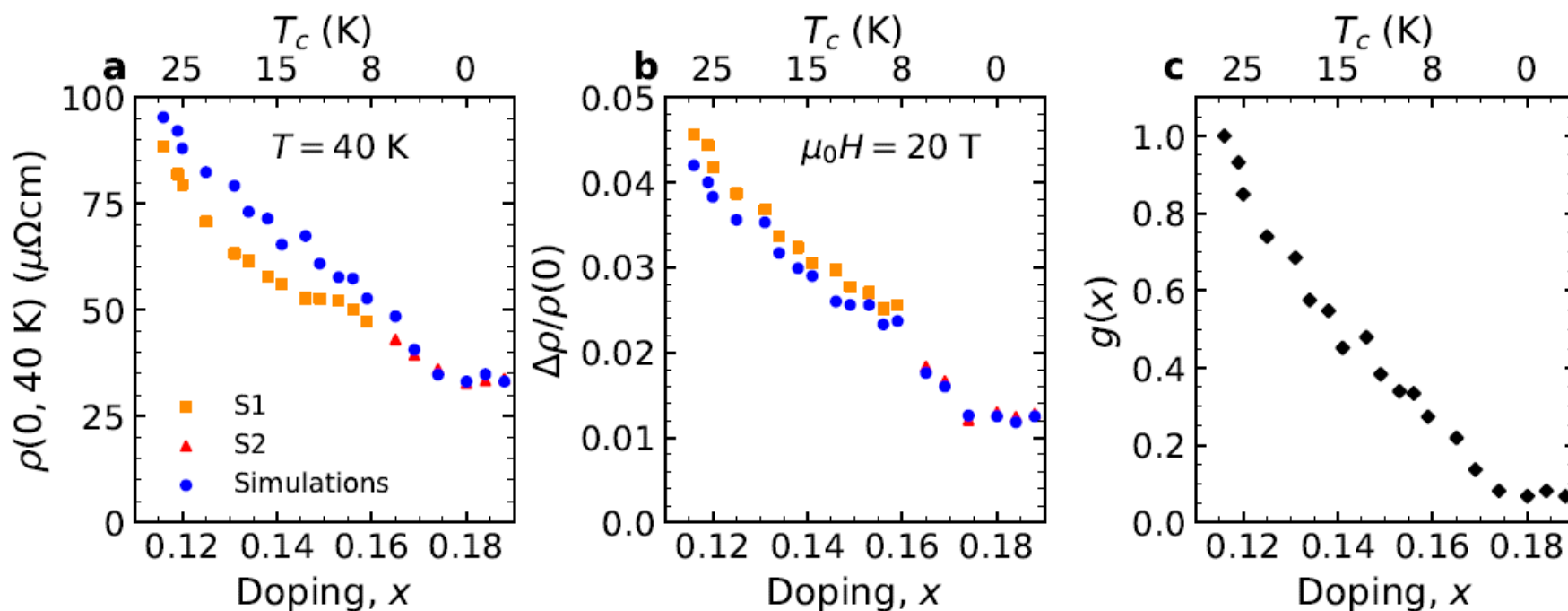
Inelastic component – reflects  $T$ -dependence of zero-field resistivity, including  $x$ -dependence of  $T$ -linear component

# Simulations $x=0.159$



# x-dependence

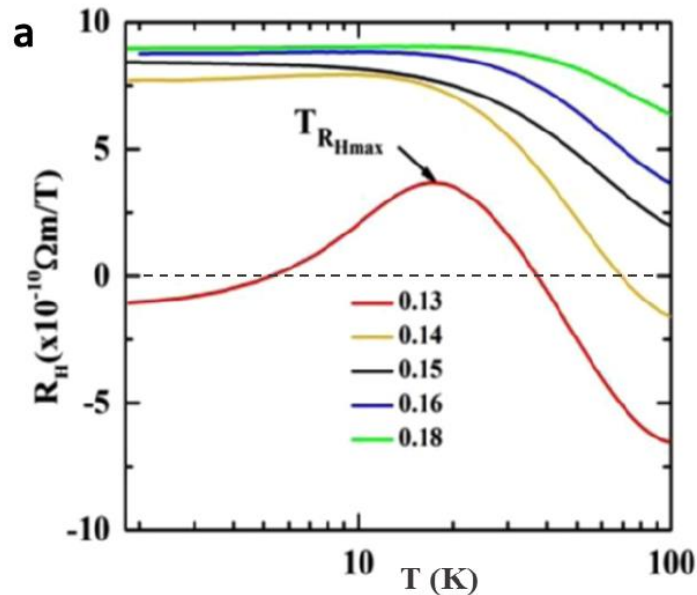
$$\tau^{-1}(\varphi, T, x) = \tau_{\text{imp}}^{-1} + \tau_{\text{HS}}^{-1}(\varphi) + g(x)\alpha_1 T \sin^2(2\varphi) + \alpha_2 T^2 \sin^2(2\varphi)$$



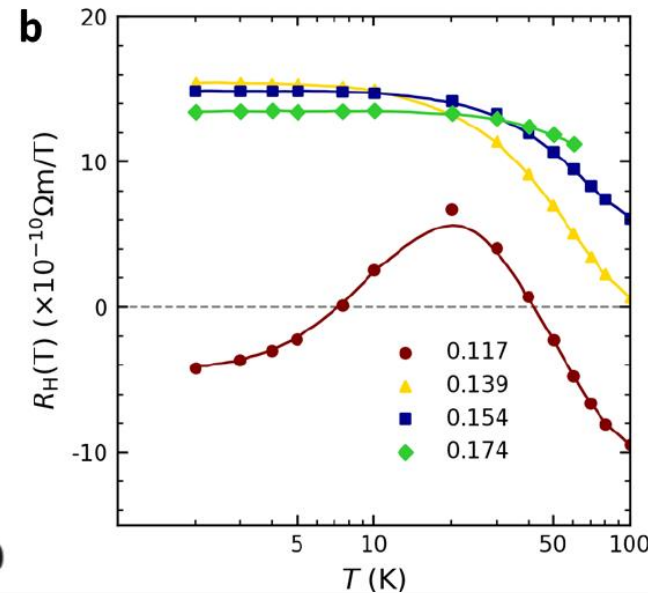
# Verifying the Scattering rate: Hall Effect

$R_H$  changes sign – even in the absence of a FSR

Use **current vertex corrections** to constrain the scattering rate



Sarkar *et al.*, PRB  
96, 155449 (2017)



Yuan *et al.*, Nature  
602, 431–436 (2022)

$$\vec{J}_k = \frac{1}{1 - \epsilon_k^2} (\vec{v}_k + \epsilon_k \vec{v}_{k \pm Q})$$

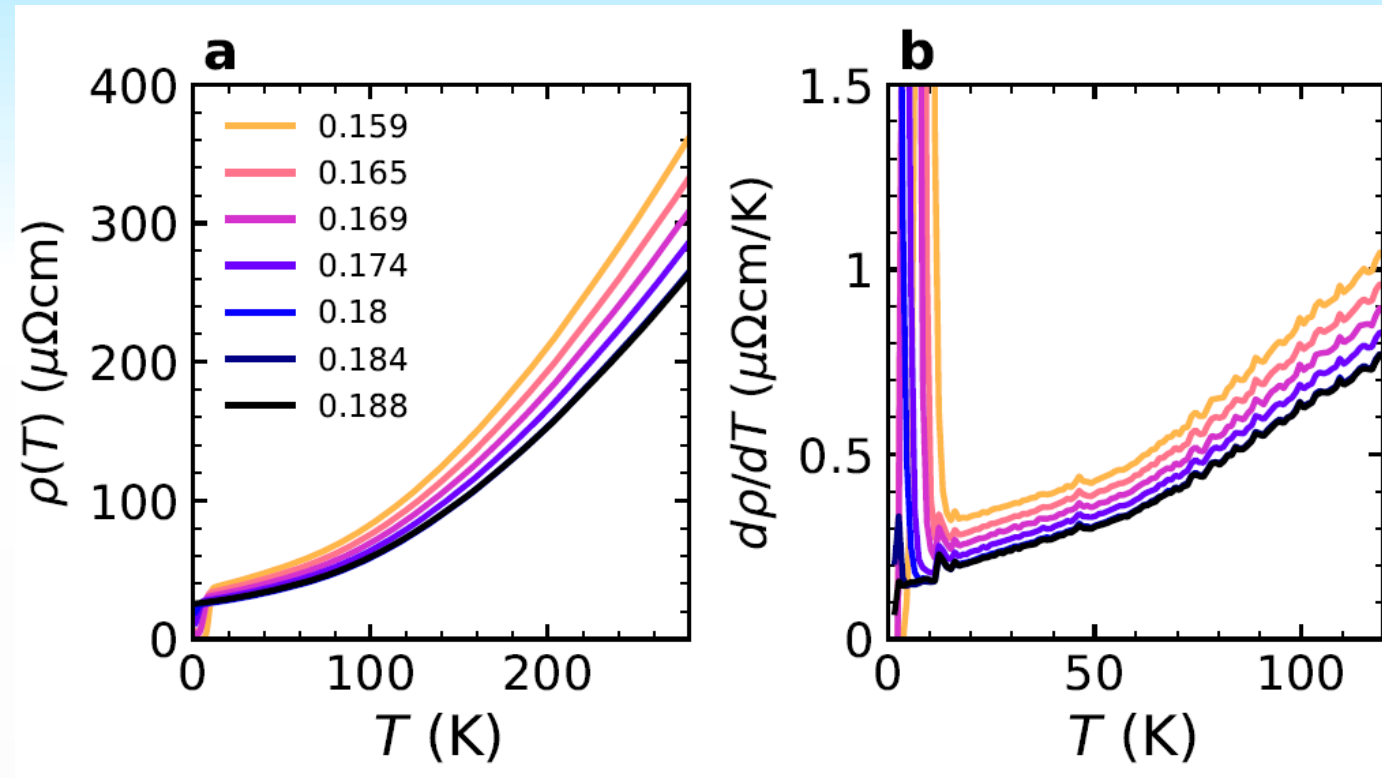
Current (hence velocity) vector at the hotspots is altered due to  $(\pi, \pi)$  scattering.

# Conclusion

- The scattering rate of LCCO is correlated with a coupling parameter which is due to antiferromagnetic spin fluctuations.
- The correlation between the coupling parameter and  $T_c$  implies that superconductivity in  $n$ -doped cuprates is mediated by antiferromagnetic spin fluctuations.
- The differences between  $n$ - and  $p$ -doped cuprates imply that the same conclusion cannot be drawn for  $p$ -doped cuprates.

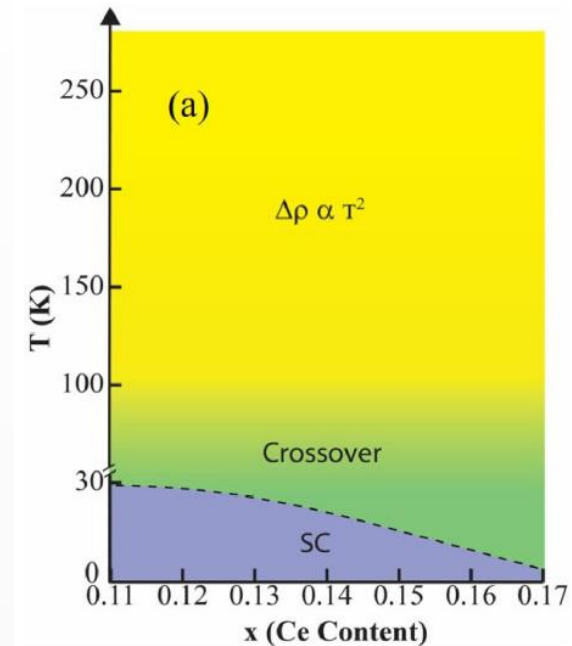
Extra slides

# Zero-field



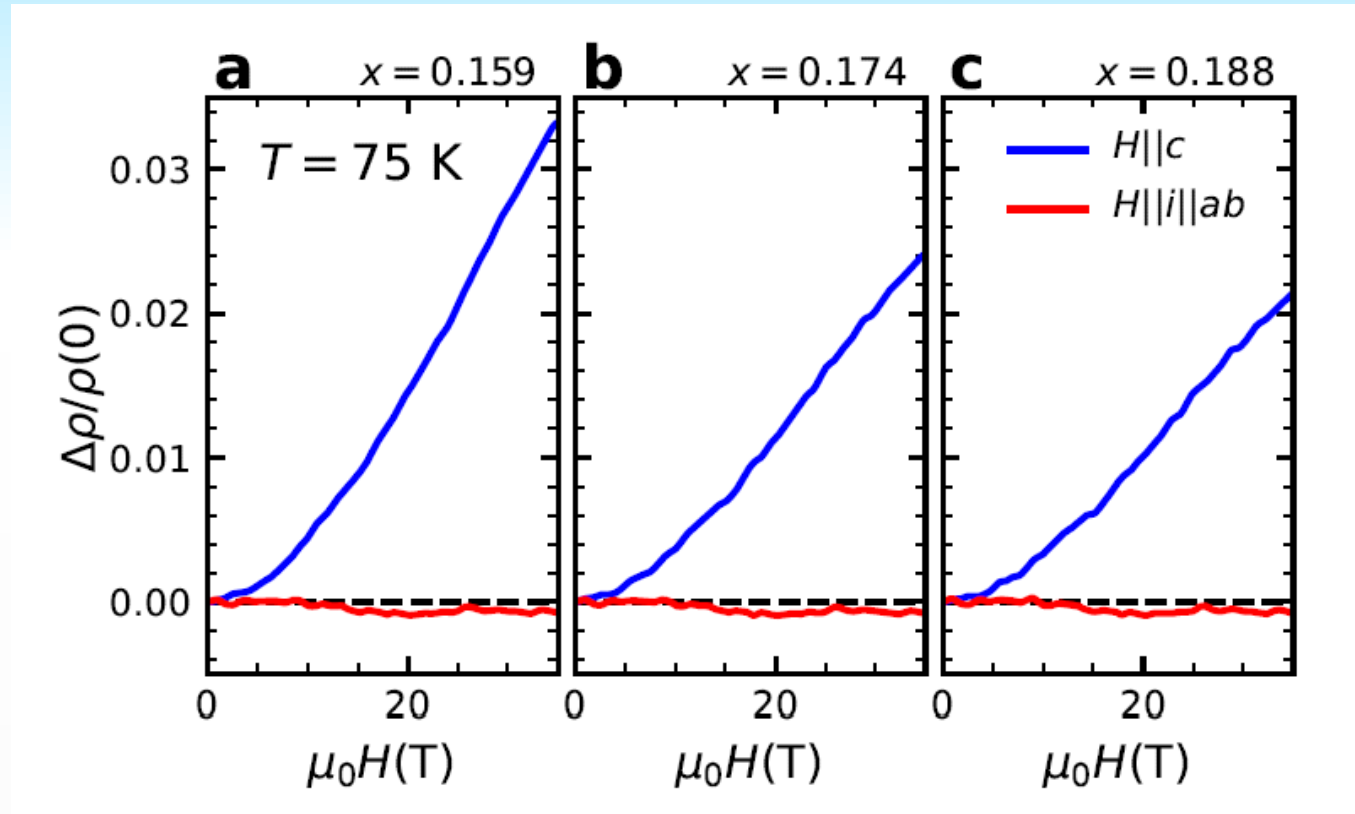
Derivative shows an  $x$ -dependent  $T$ -linear component of the resistivity and an  $x$ -independent  $T^2$  component below 70 K

T. Sarkar *et al.*, PRB  
98, 224503 (2018)



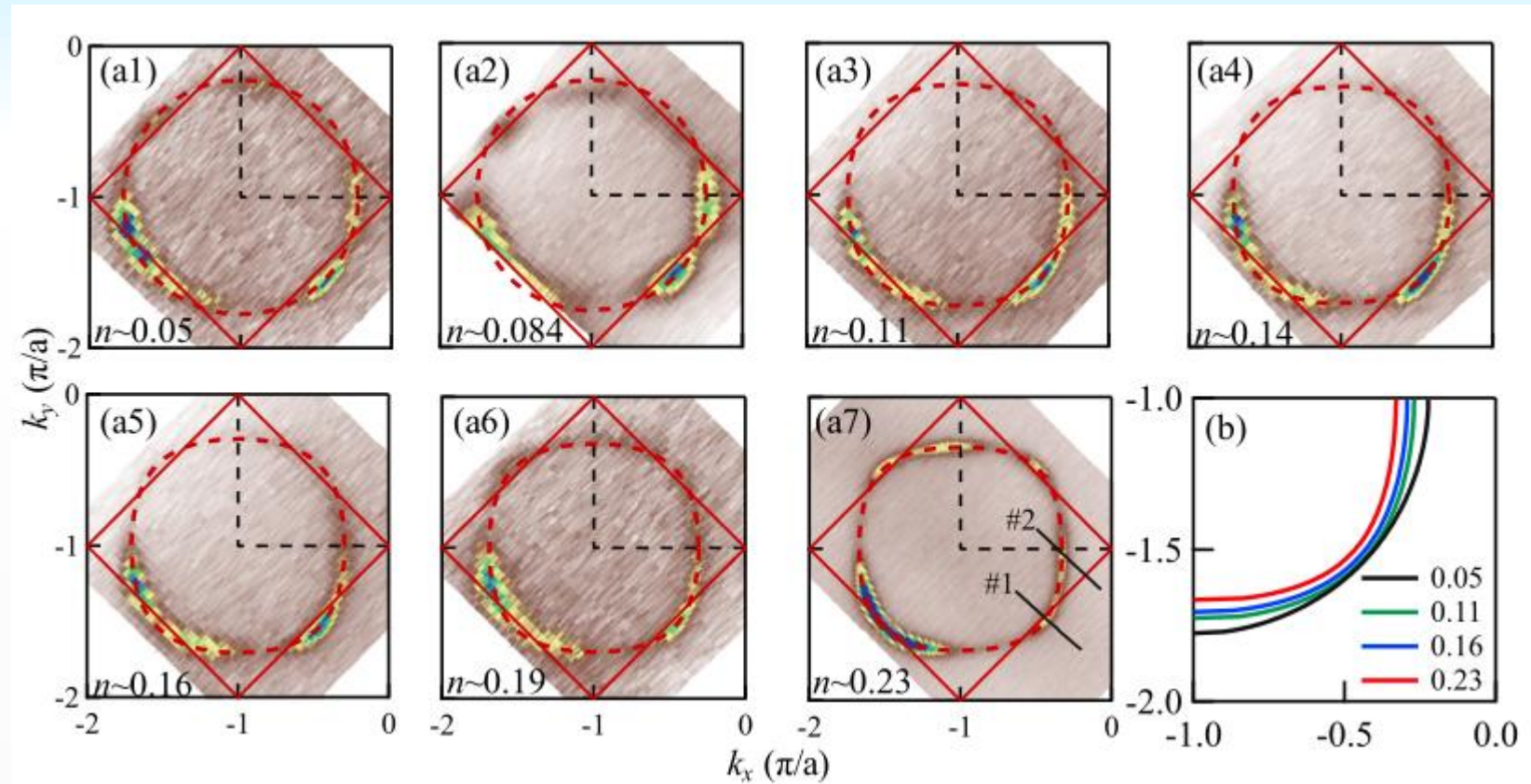


# Magnetoresistance



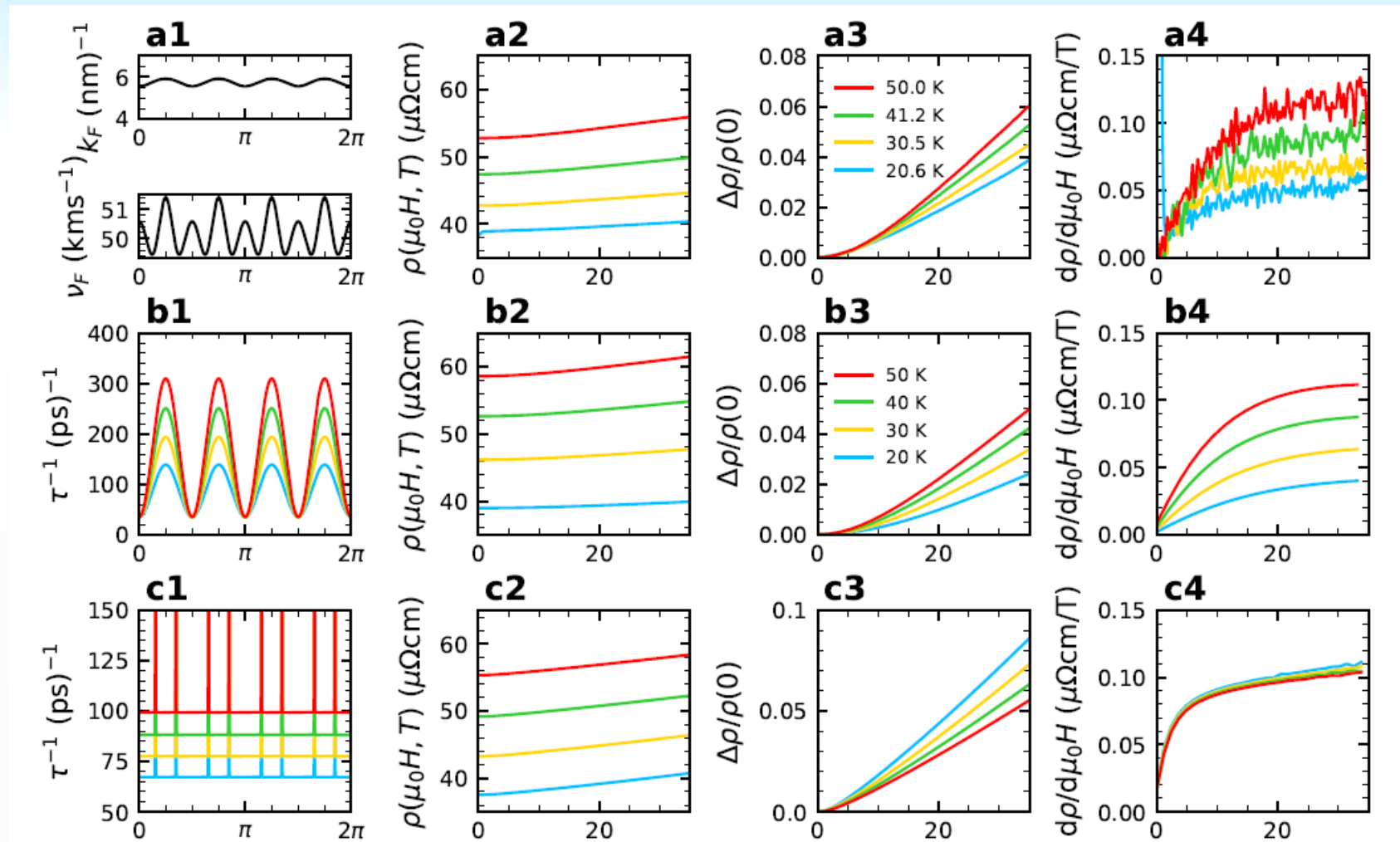
Anisotropic MR...

# Fermiology of LCCO from ARPES

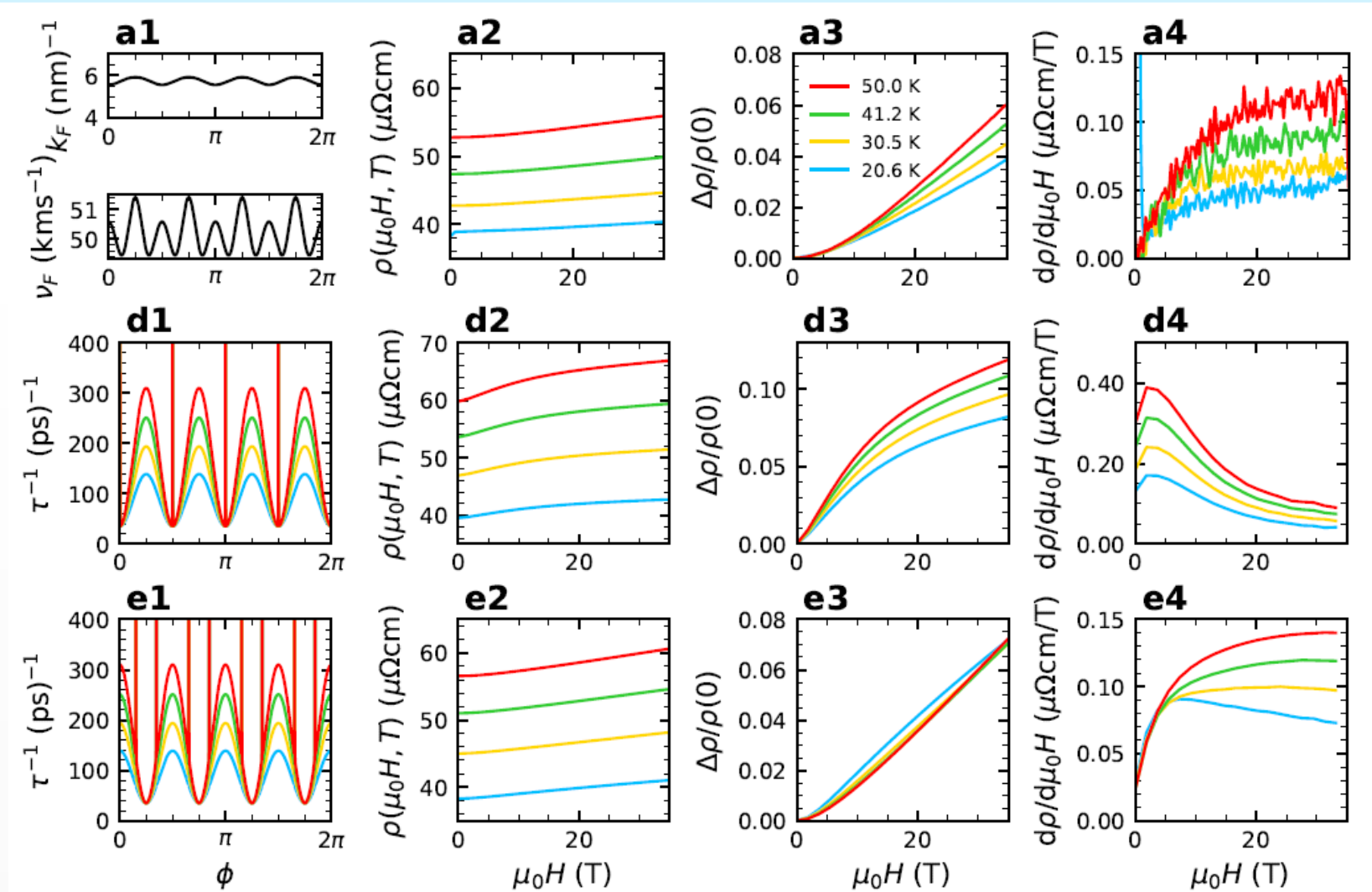


Tang *et al.*, *PRB* **104**, 155125 (2021)

# Testing other scattering rates



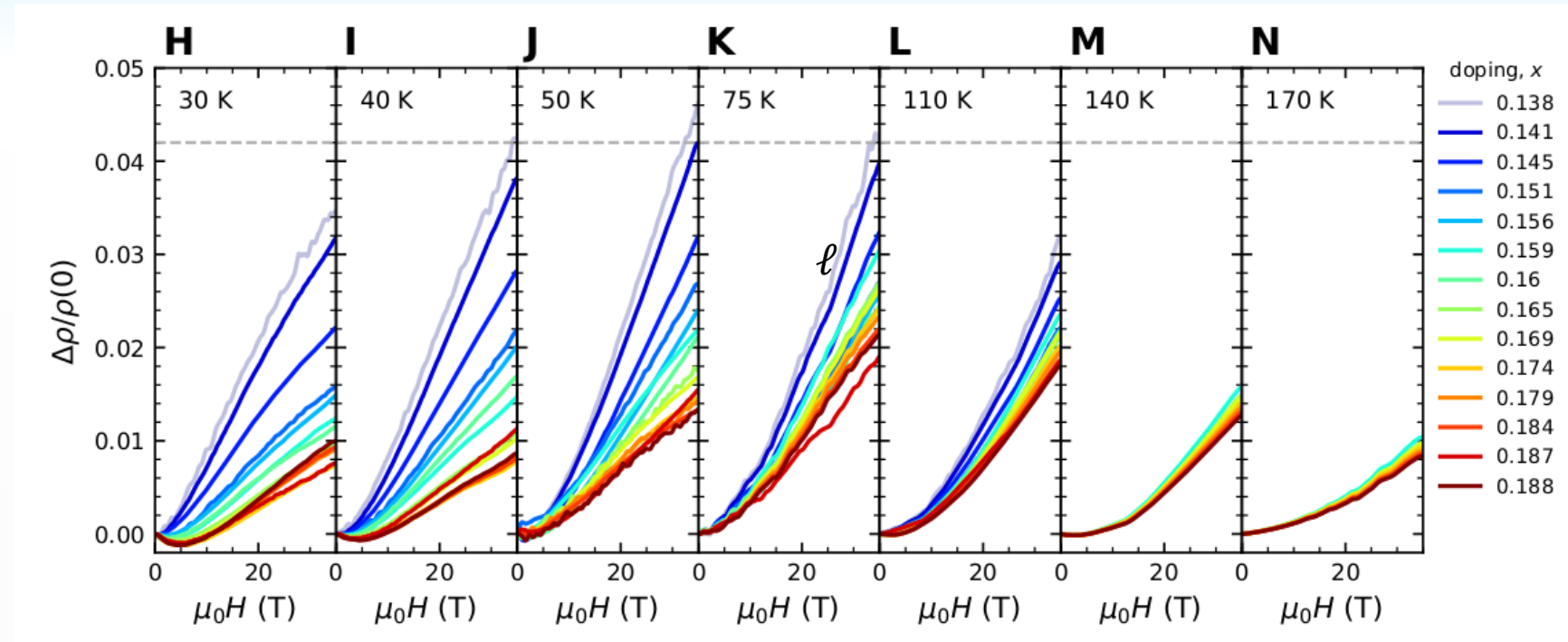
# Testing other scattering rates



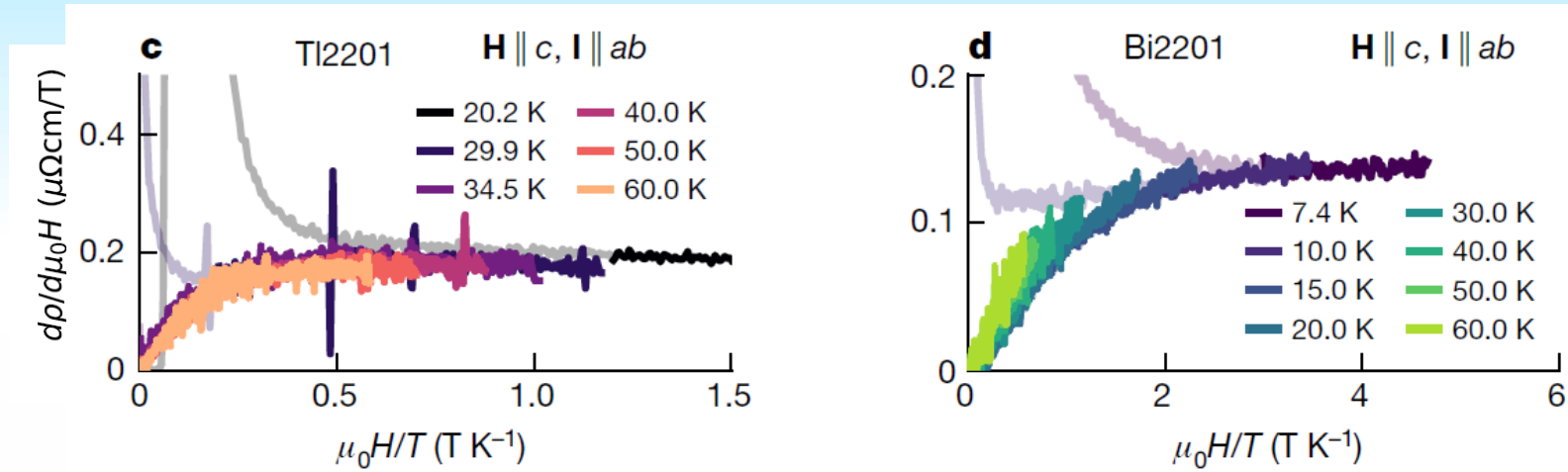
# Comparison between $n$ - and $p$ -doped

	$p$ -doped	$n$ -doped
$\rho(T) \sim T$	Yes - all $T$	Yes - $T < 20$ K
Planckian	Yes	No
$H$ -linear MR	Yes	Yes
Kohler's scaling	No	No
$H/T$ scaling	Yes	No
Orientation independent	Yes	No
$T$ -independent slope	Yes	No

# Film 2 – MR



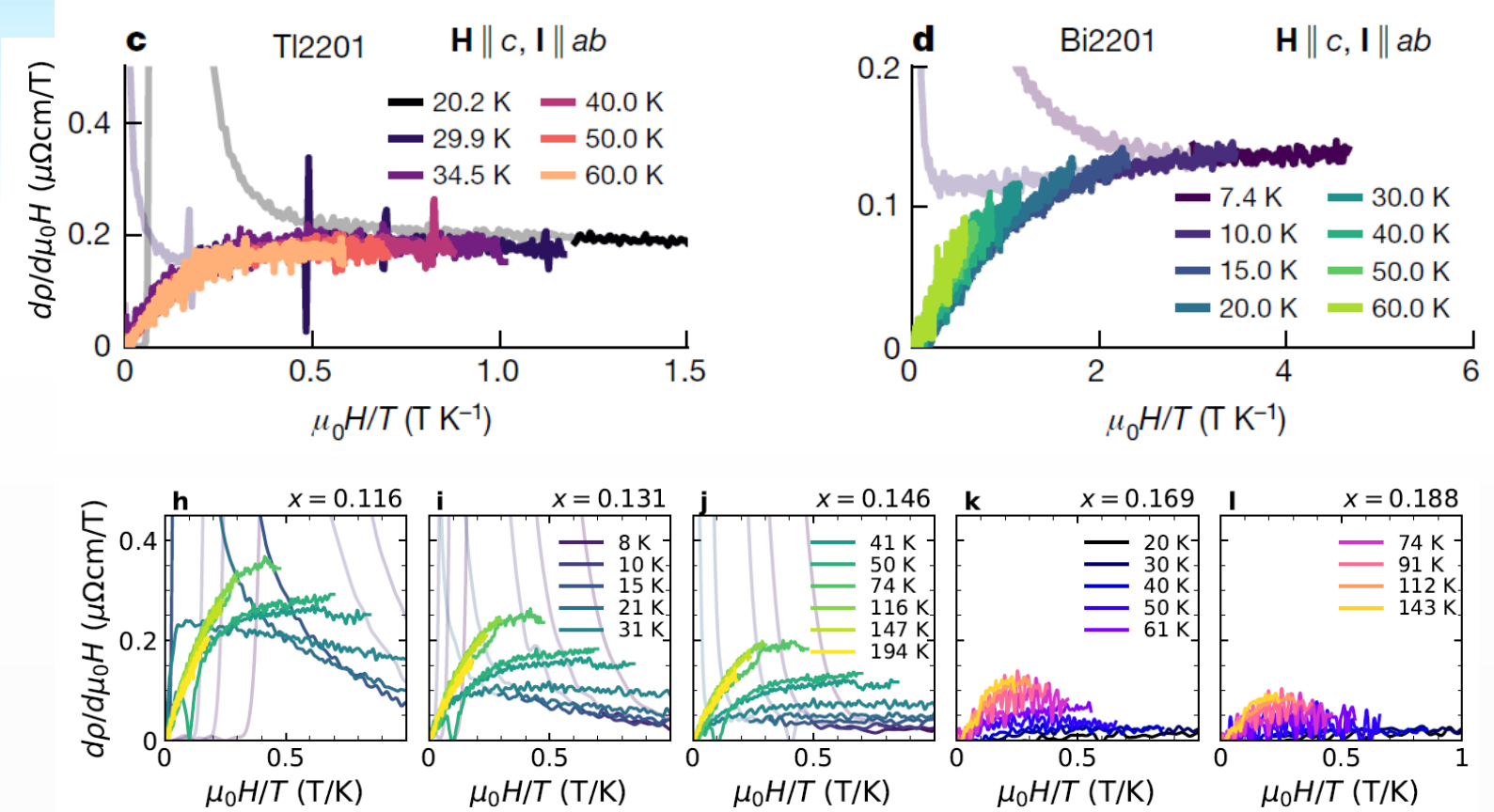
# Magnetoresistance



Ayres, Berben *et al.*,  
Nature **595**, 661 (21)

*p*-doped :  $H/T$  quadrature scaling indicative of incoherent carriers

# Magnetoresistance

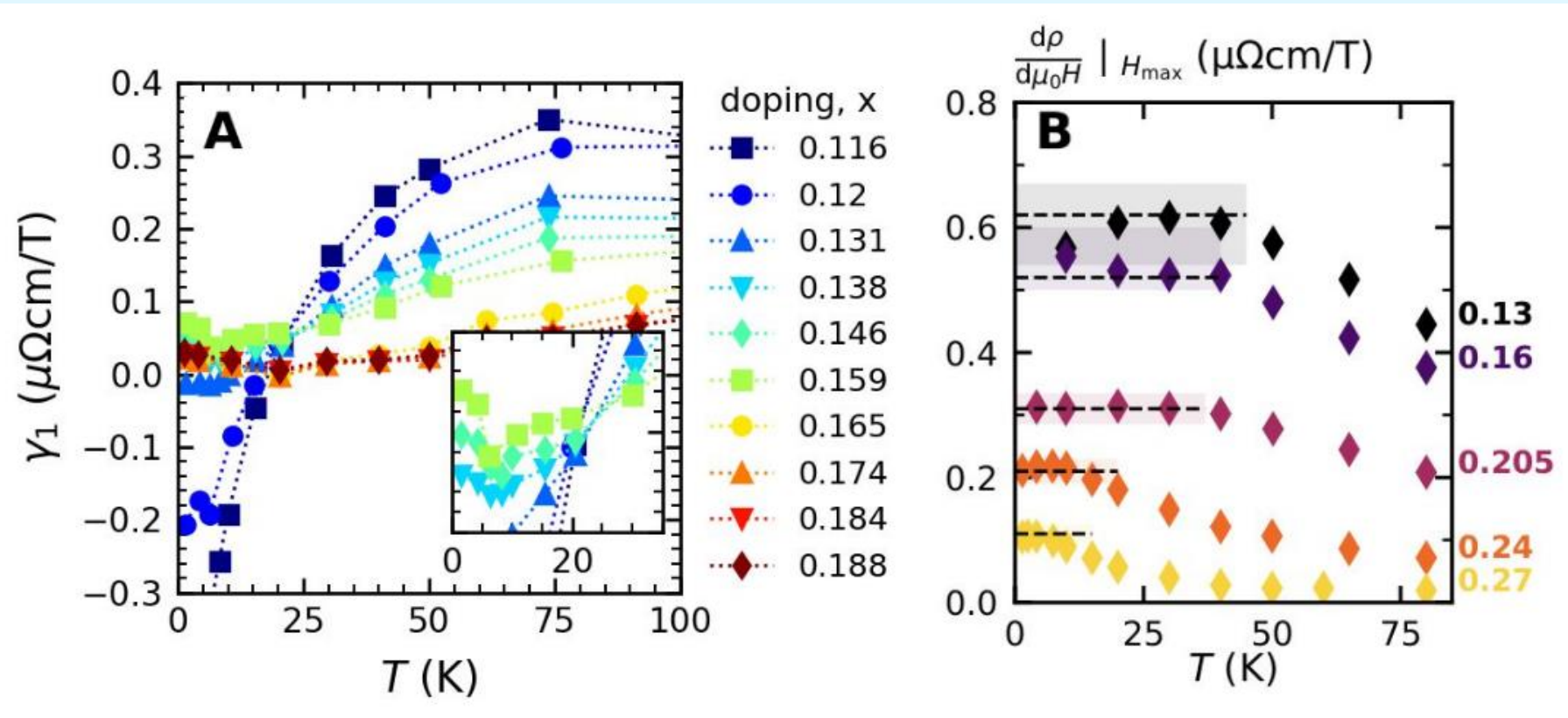


Ayres, Berben *et al.*,  
Nature **595**, 661 (21)

*n*-doped :  $H/T$  scaling breaks down at an  $x$ -independent  $T \sim 70$  K



# Magnetoresistance

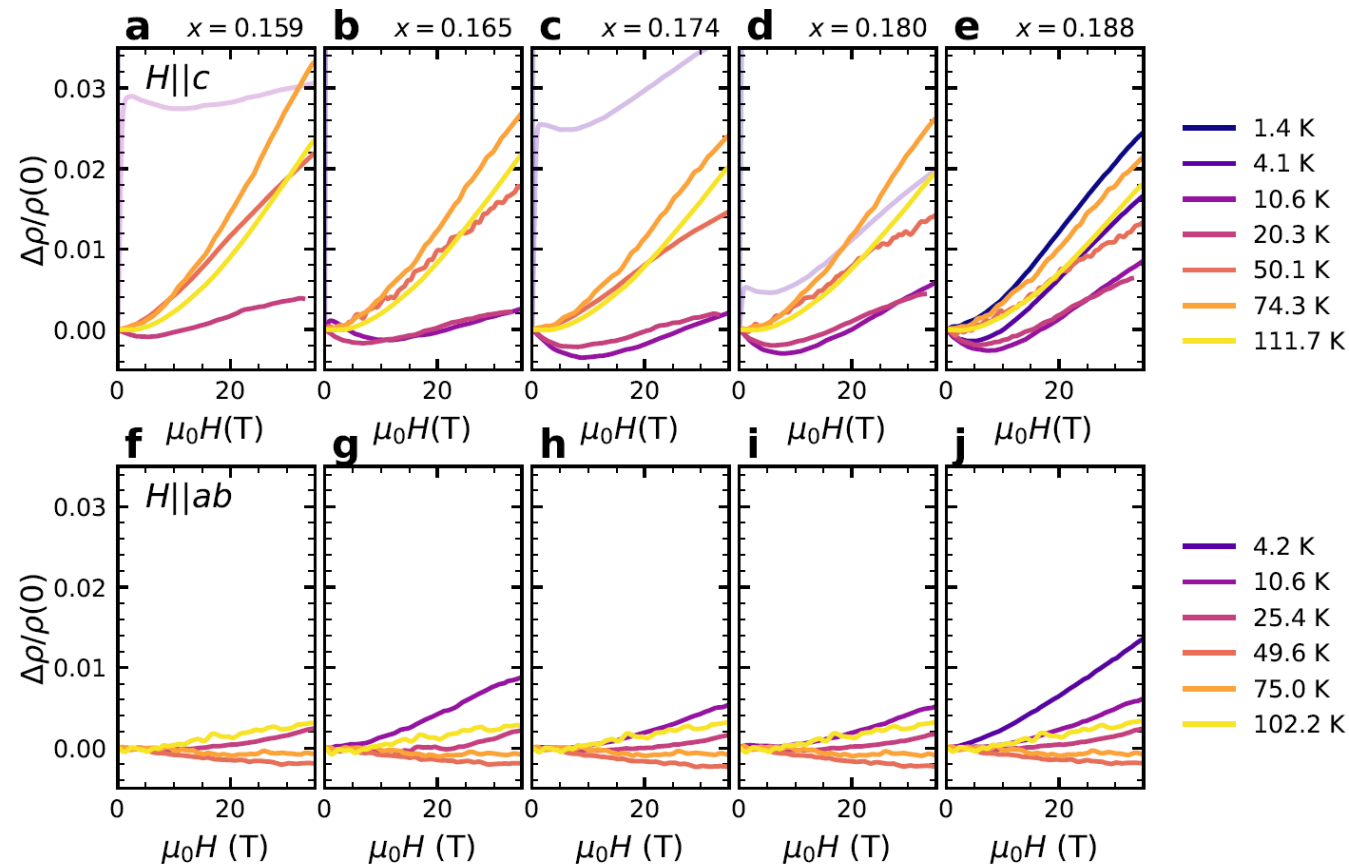


MR between 30-33 T

$p$ -doped: slope becomes constant at low- $T$

$n$ -doped: slope never becomes constant

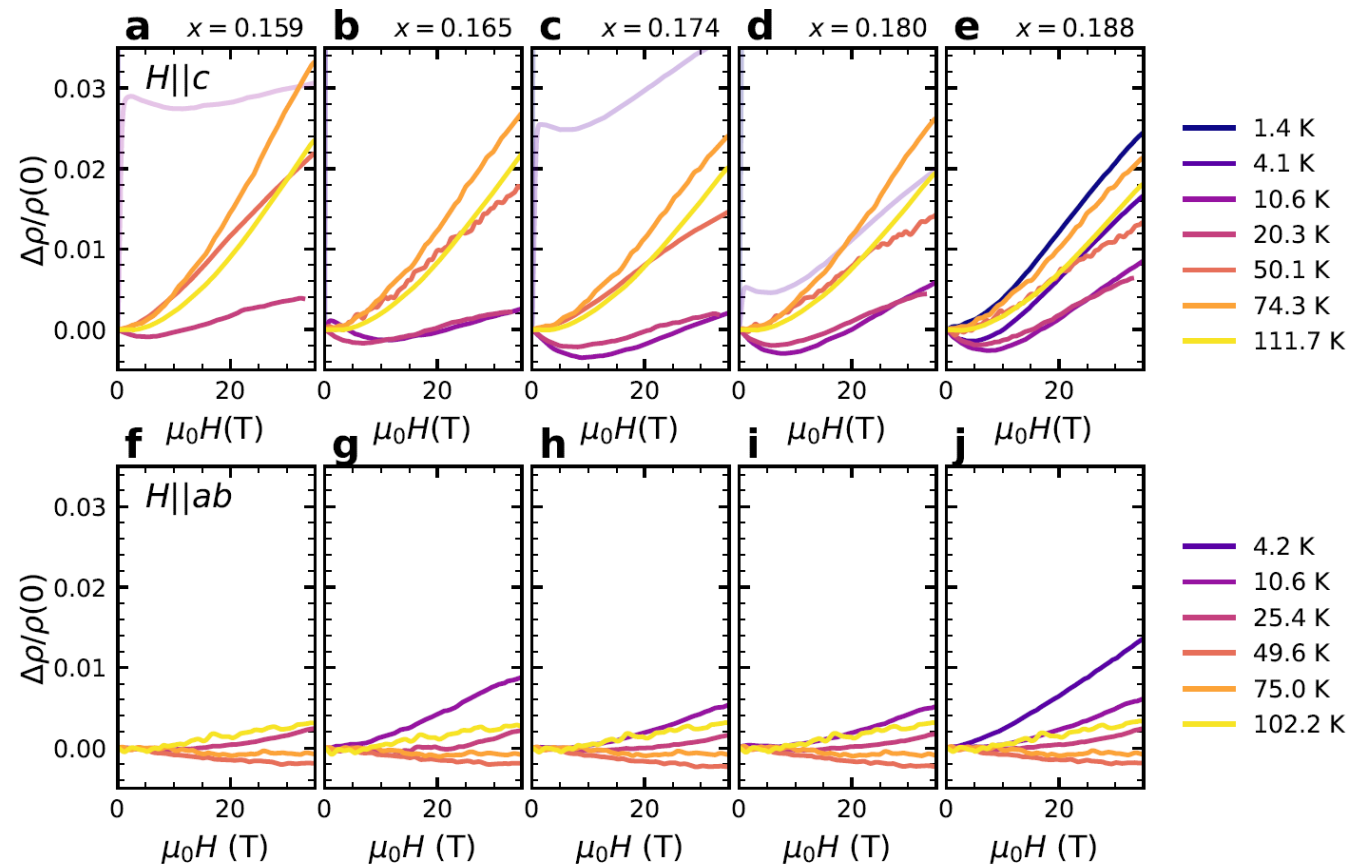
# In-plane MR



MR is anisotropic – as is expected from a Lorentz-force free configuration.

This, again, is in stark contrast to the  $p$ -doped cuprates.

# In-plane MR



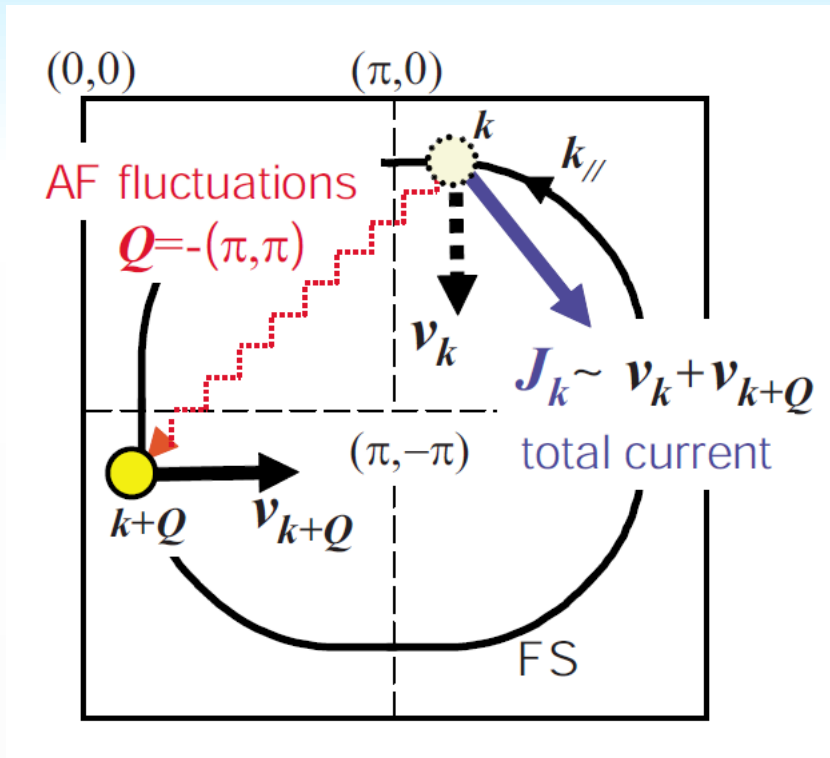
MR is anisotropic – as is expected from a Lorentz-force free configuration.

This, again, is in stark contrast to the  $p$ -doped cuprates.

This begs the question:

*Can the MR of  $n$ -doped cuprates be described within a conventional framework?*

# Current vertex corrections



$$\sigma_{xy} = \frac{-e^3 B}{2\pi^2 \hbar^2 c} \int_0^{2\pi} \ell_x \frac{\partial \ell_y}{\partial \varphi} d\varphi$$

Scattering between two points causes a modification of the velocity vector at those two points

G. Jenkins *et al.*, PRB **81**, 024508 (2010)  
 H. Kontani, Rep. Prog. Phys. **71**, 026501 (2008)

# Current vertex corrections

$$\sigma_{xy} = \frac{-e^3 B}{2\pi^2 \hbar^2 c} \int_0^{2\pi} \ell_x \frac{\partial \ell_y}{\partial \varphi} d\varphi$$

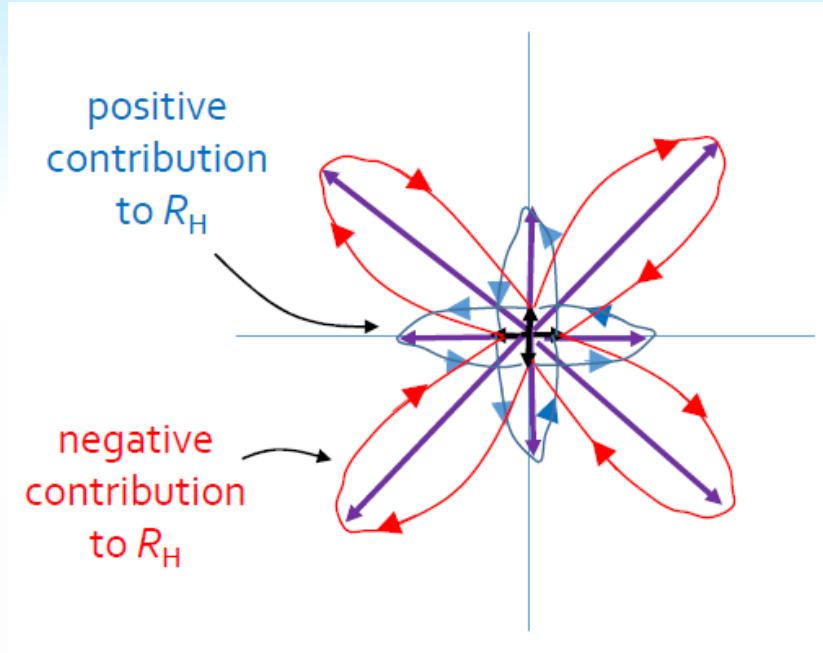
$$\ell \propto v_F$$

→ A change in  $v_F$  causes a change in  $\ell$

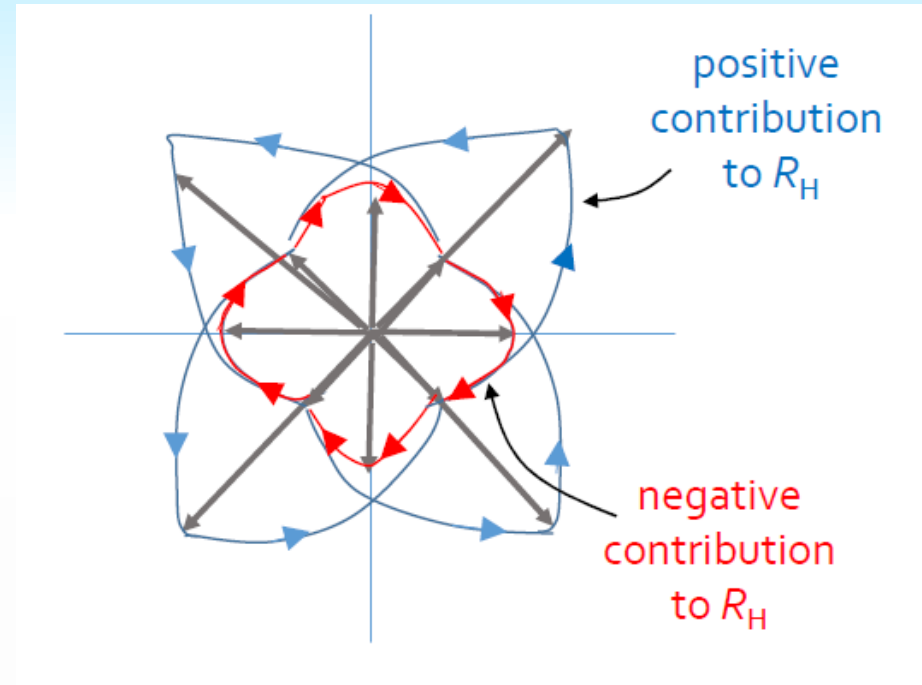
Could this help distinguish between hotspots at the antinodes and hotspots at the AFMBZ boundary?

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# Current vertex corrections



AN hotspots  
Charge CVCs



AFMBZ hotspots  
Spin CVCs

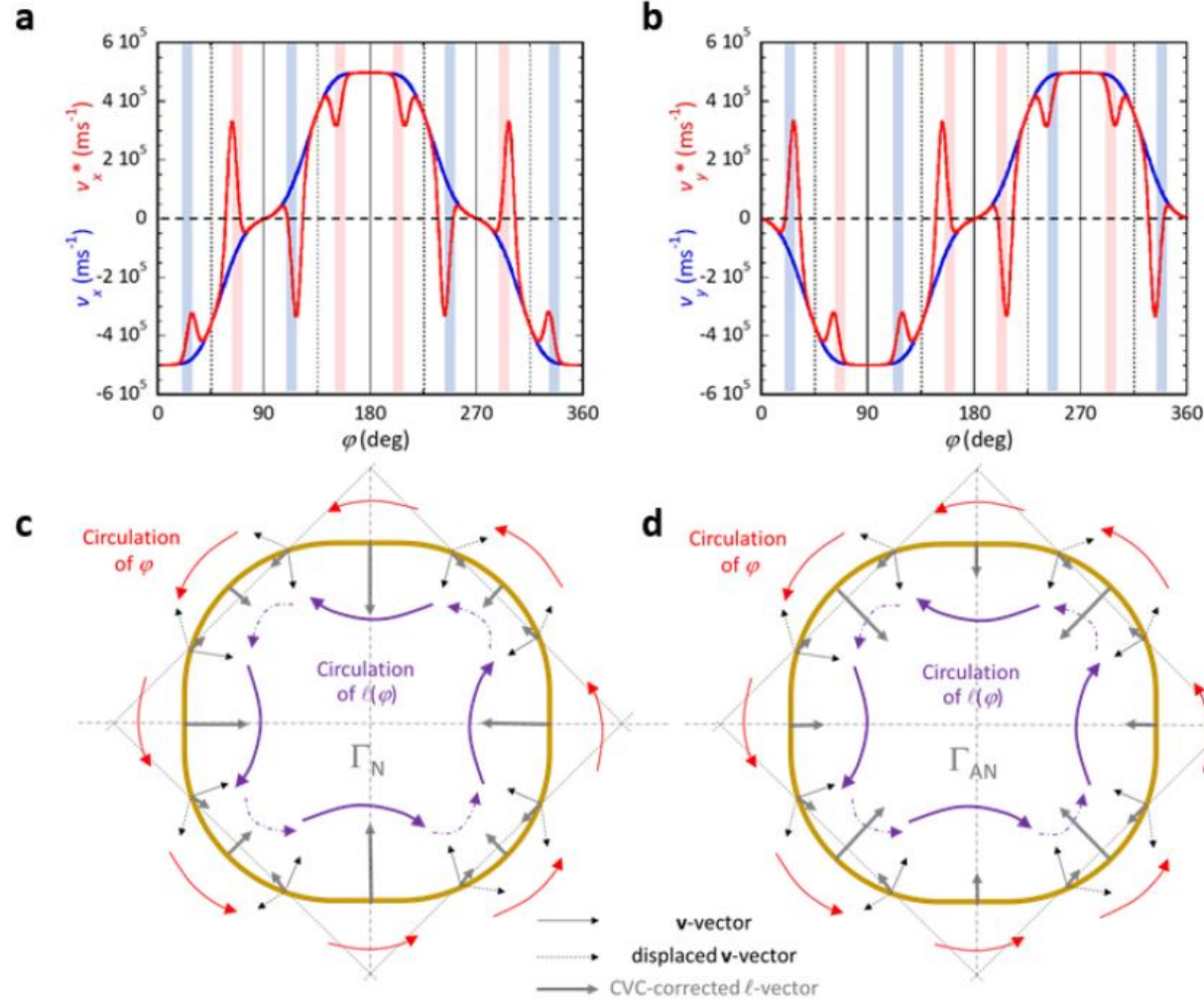
If employing CVCs can account for the sign change in  $R_H$ , we can distinguish between spin and charge...  
→ Work in progress!

# CVCs

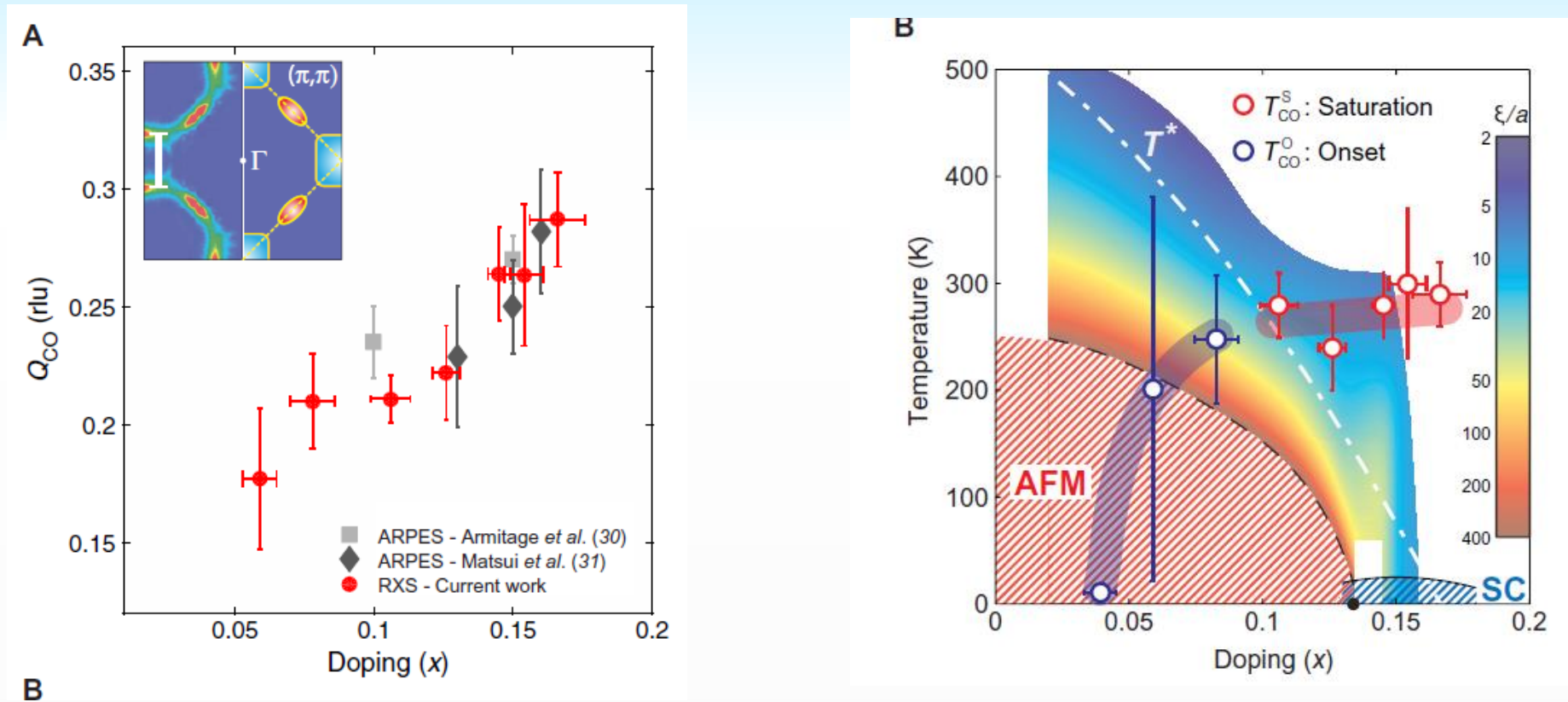
$$\left[ \begin{array}{l} v_x^* \text{ negative +} \\ \frac{\partial(v_y^*)}{\partial\varphi} \text{ positive} \end{array} \right.$$

$$\sigma_{xy} \approx \oint v_x^* \tau \cdot \frac{\partial(v_y^* \tau)}{\partial\varphi} d\varphi$$

$$\left[ \begin{array}{l} v_x^* \text{ positive +} \\ \frac{\partial(v_y^*)}{\partial\varphi} \text{ negative} \end{array} \right.$$

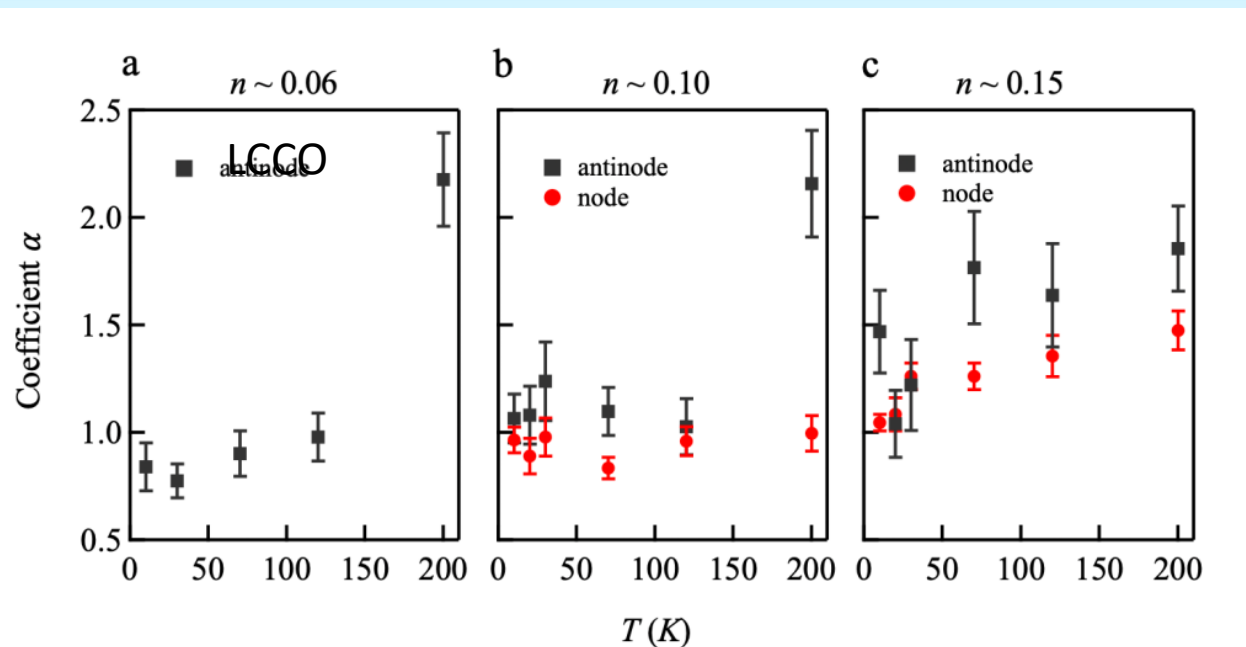


# Charge order in $n$ -doped cuprates

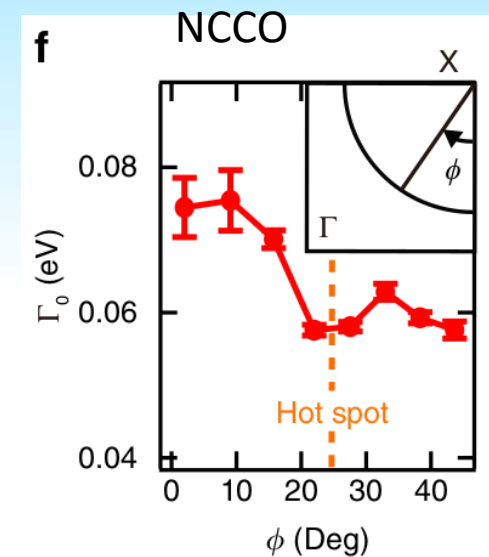




# Experimentally-derived scattering rate



C. Y. Tang *et al.*, npj Quant. Mater (2022)



Horio *et al.*, Nat. Commun 2016

He *et al.*, PNAS (2018)

